Extremely High-Energy Cosmic & Relic Neutrinos

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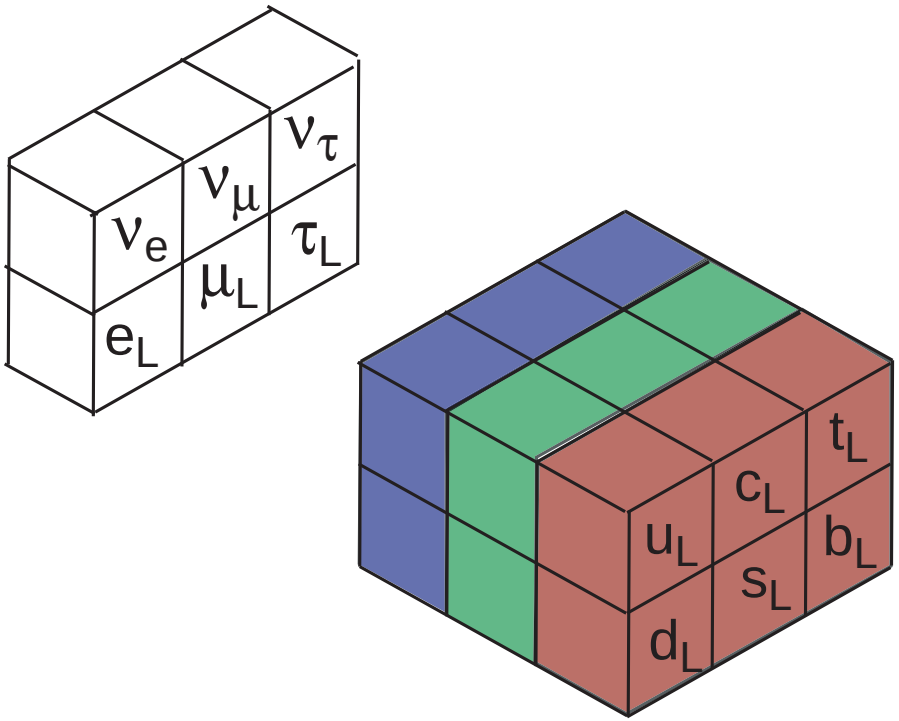
Neutrinos are abundant!

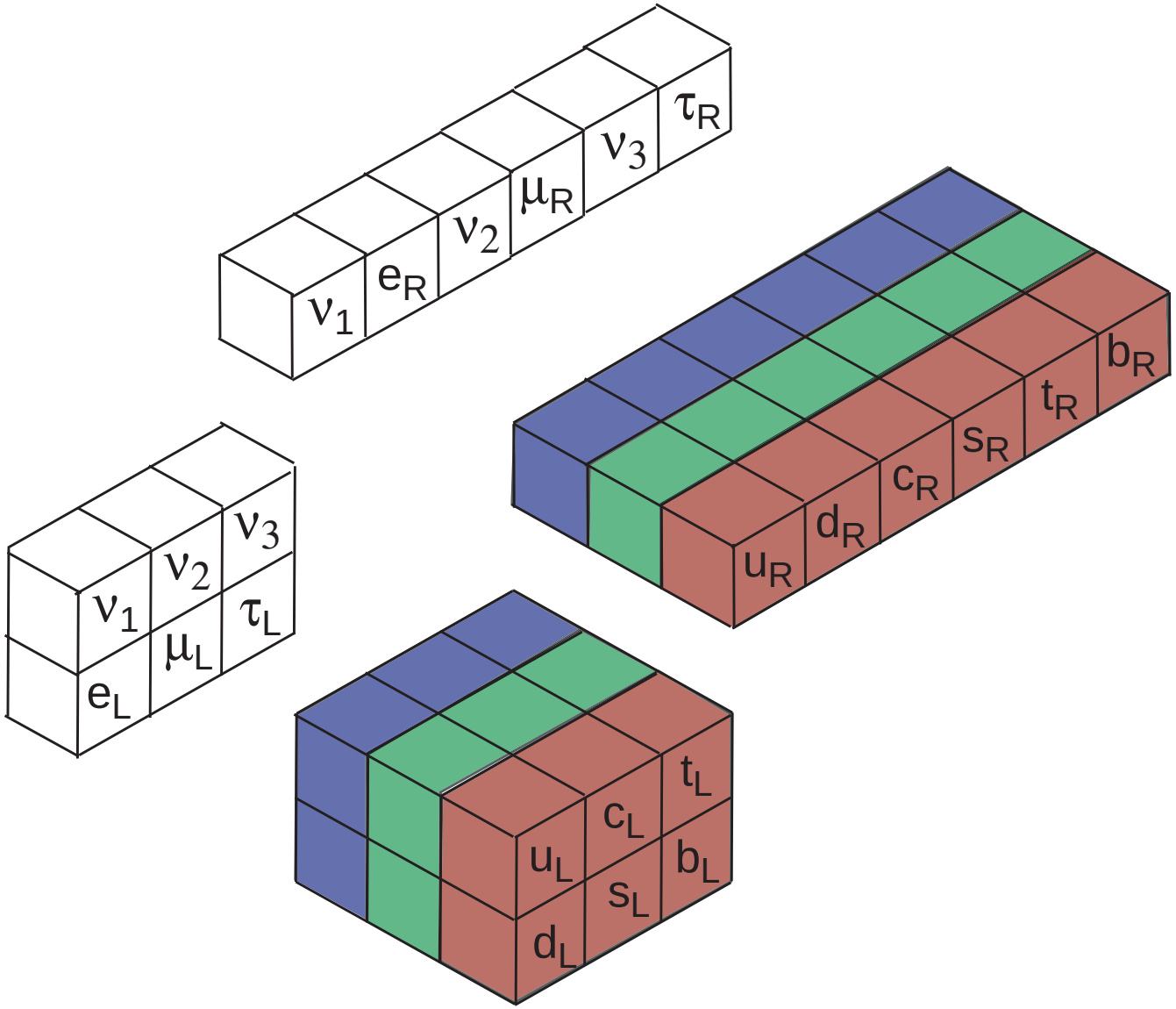
- Each second, some 10^{14} neutrinos made in the Sun pass through your body.
- Each second, about 10^3 neutrinos made in Earth's atmosphere by cosmic rays pass through your body.
- Other neutrinos reach us from natural (radioactive decays of elements inside the Earth) and artificial (nuclear reactors, particle accelerators) sources.
- Inside your body are more than 10^7 neutrino relics from the early universe.

$\nu_i,\ \bar{\nu}_i$ number density now: 56 cm^{-3}, $\propto (1+z)^3$

Neutrinos in the electroweak theory



Neutrinos in the electroweak theory



Leptons are observed as free particles

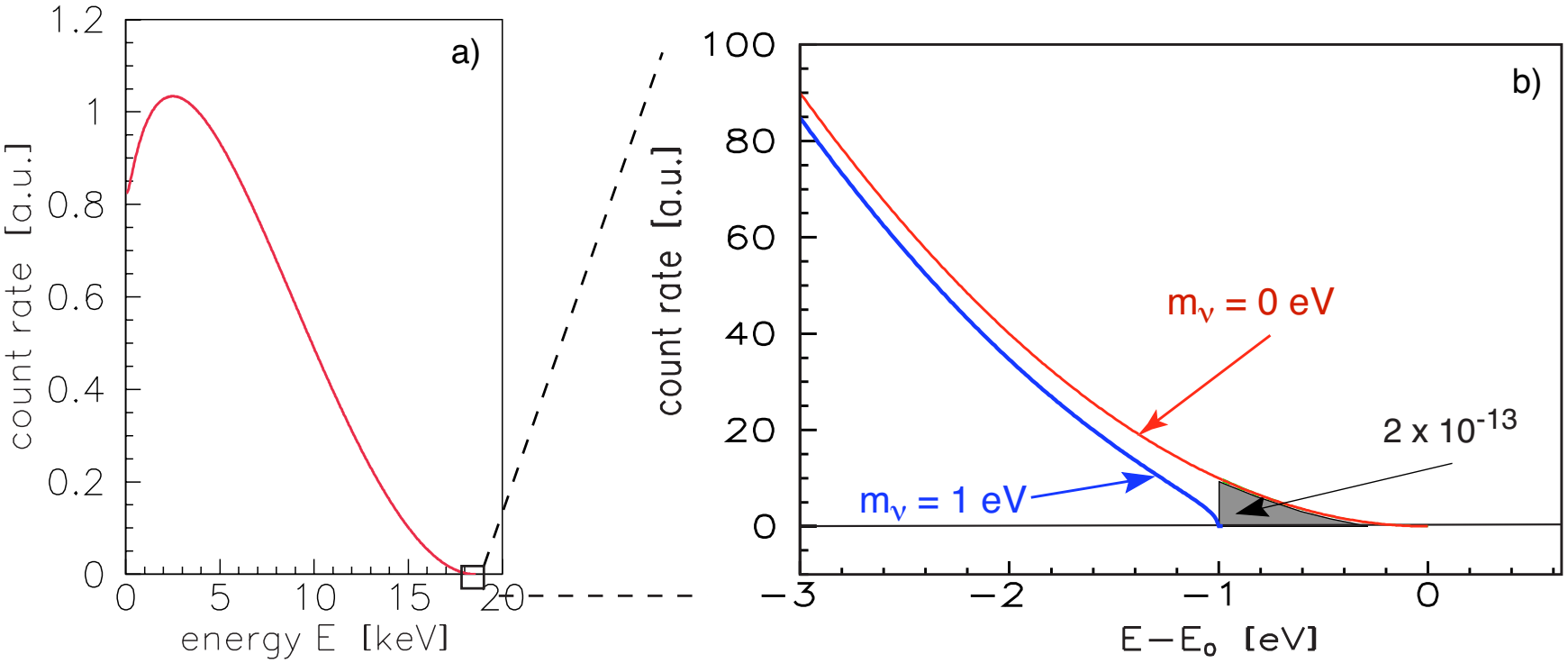
Lepton	Mass	Lifetime
ν_e	< 2 eV	
e^-	0.510 998 918(44) MeV	$> 4.6 \times 10^{26}$ y (90% CL)
ν_μ	< 0.19 MeV (90% CL)	
μ^-	105.658 369 2(94) MeV	$2.197\,03(4) \times 10^{-6}$ s
ν_τ	< 18.2 MeV (95% CL)	
τ^-	1776.90 ± 0.20 MeV	$290.6 \pm 1.0 \times 10^{-15}$ s

All spin-$\frac{1}{2}$, pointlike ($\lesssim$ few $\times 10^{-17}$ cm)

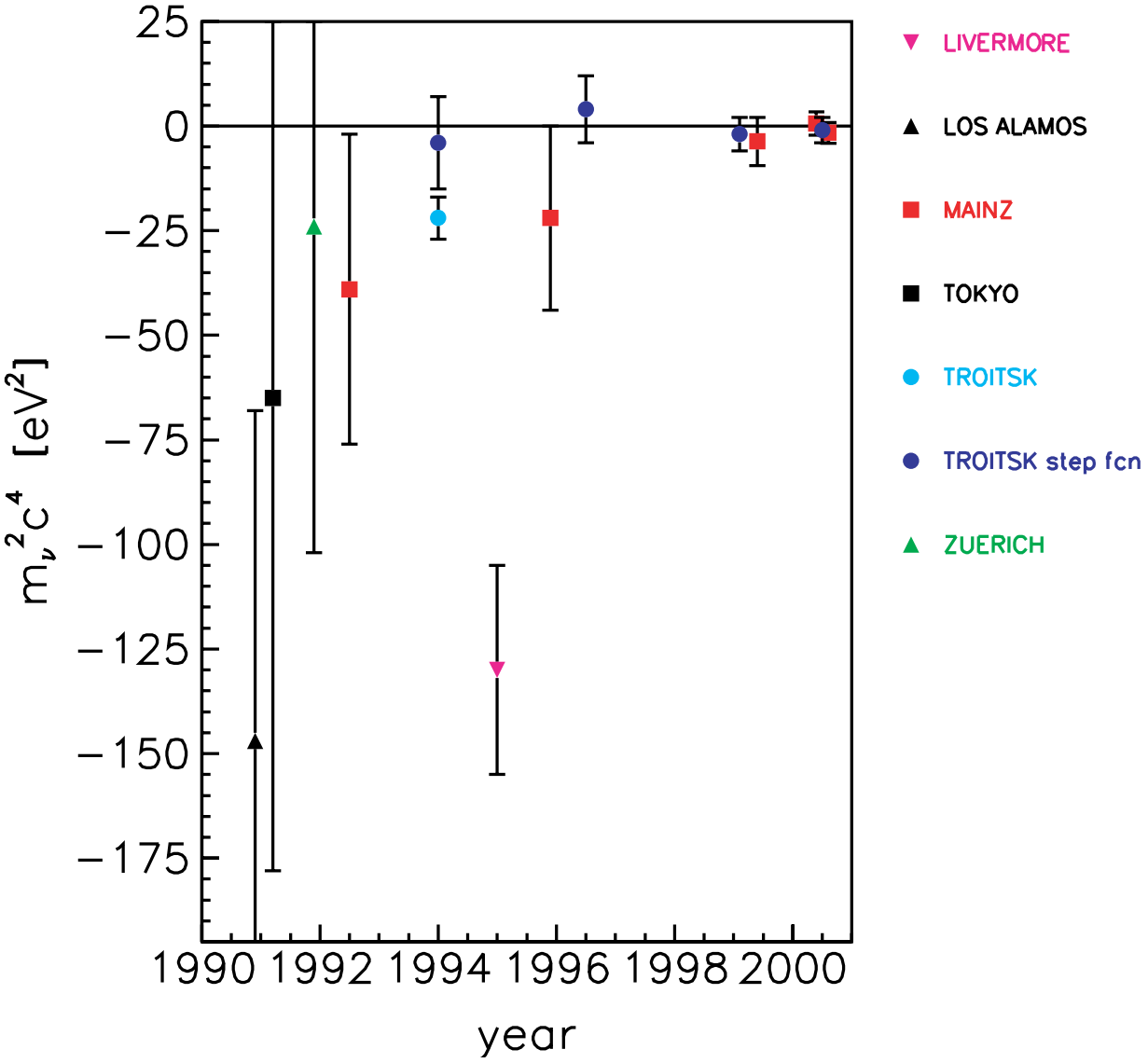
kinematically determined ν masses consistent with 0
(ν oscillations $\Rightarrow$ nonzero, unequal masses)

Tritium β-decay spectrum

$$^3\mathrm{H} \rightarrow {}^3\mathrm{He}\ e^-\ \bar{\nu}_e\colon\ Q \approx 18.57\ \mathrm{keV}$$

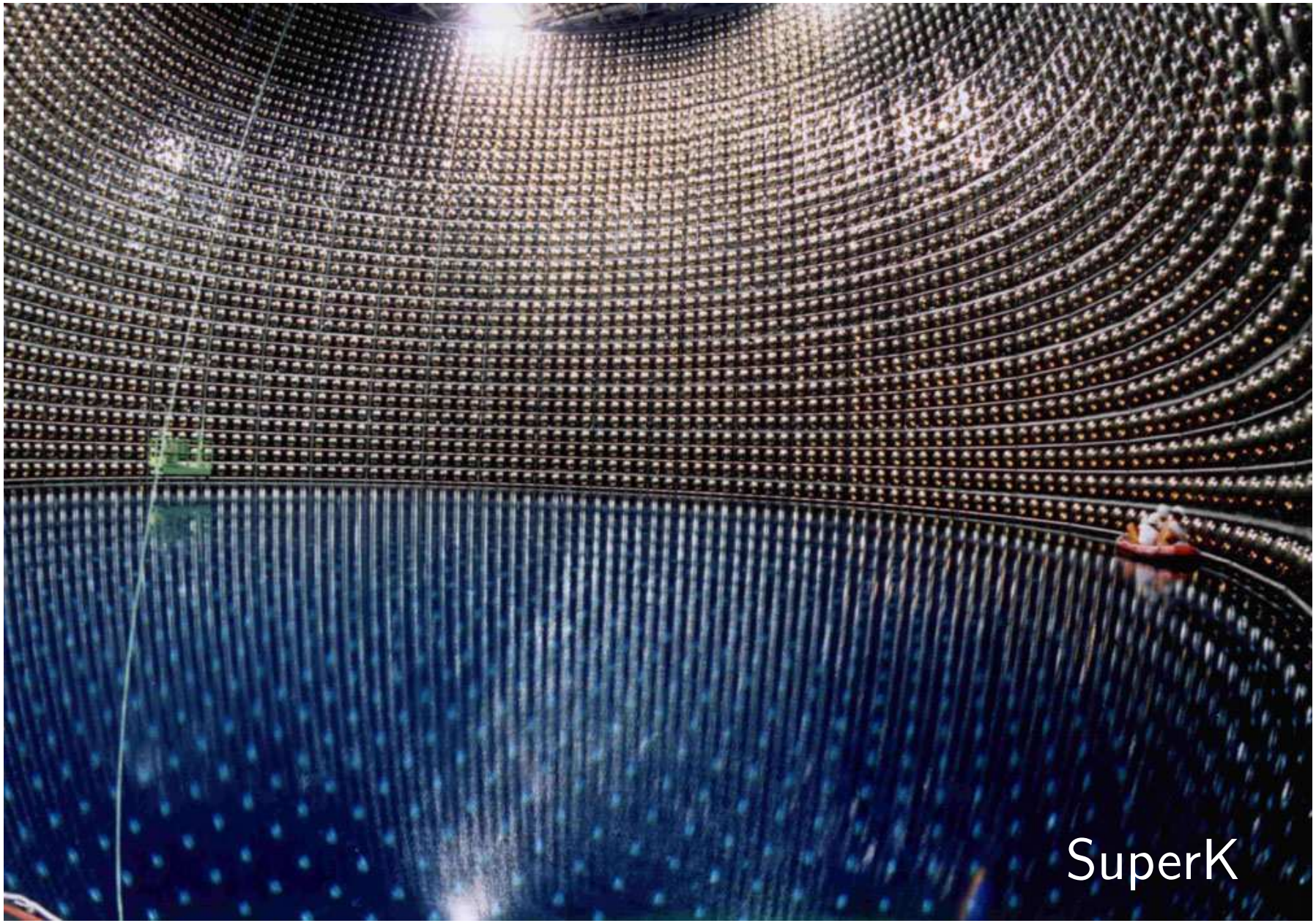


ν mass limits (e-associated)



KATRIN aims for $m_\nu \lesssim 0.2$ eV

Neutrino flavor change $\rightsquigarrow$ neutrinos have mass



The essence of neutrino oscillations

If neutrinos of definite flavor $(\nu_e, \nu_\mu, \nu_\tau)$ are superpositions of different mass eigenstates (ν_1, ν_2, ν_3)
the mass eigenstates evolve in time with different frequencies . . . and so the superposition changes in time

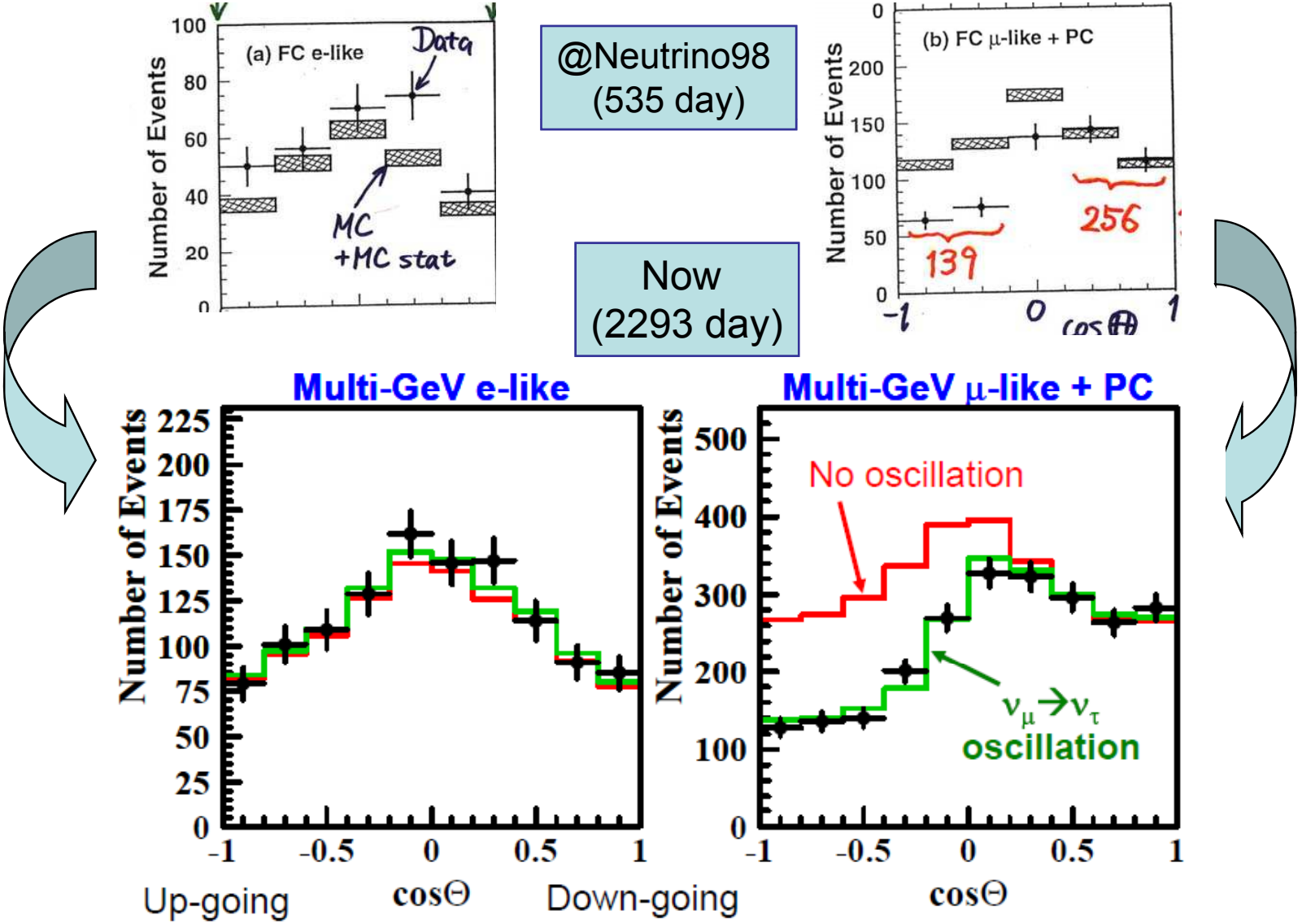
$\boxed{\text{Beam created as flavor } \nu_\alpha \text{ evolves into a flavor mixture}}$

Suppose $\nu_\alpha = \nu_1 \cos\theta + \nu_2 \sin\theta$; $\nu_\beta = -\nu_1 \sin\theta + \nu_2 \cos\theta$:

After distance L, beam created as ν_α with energy E has

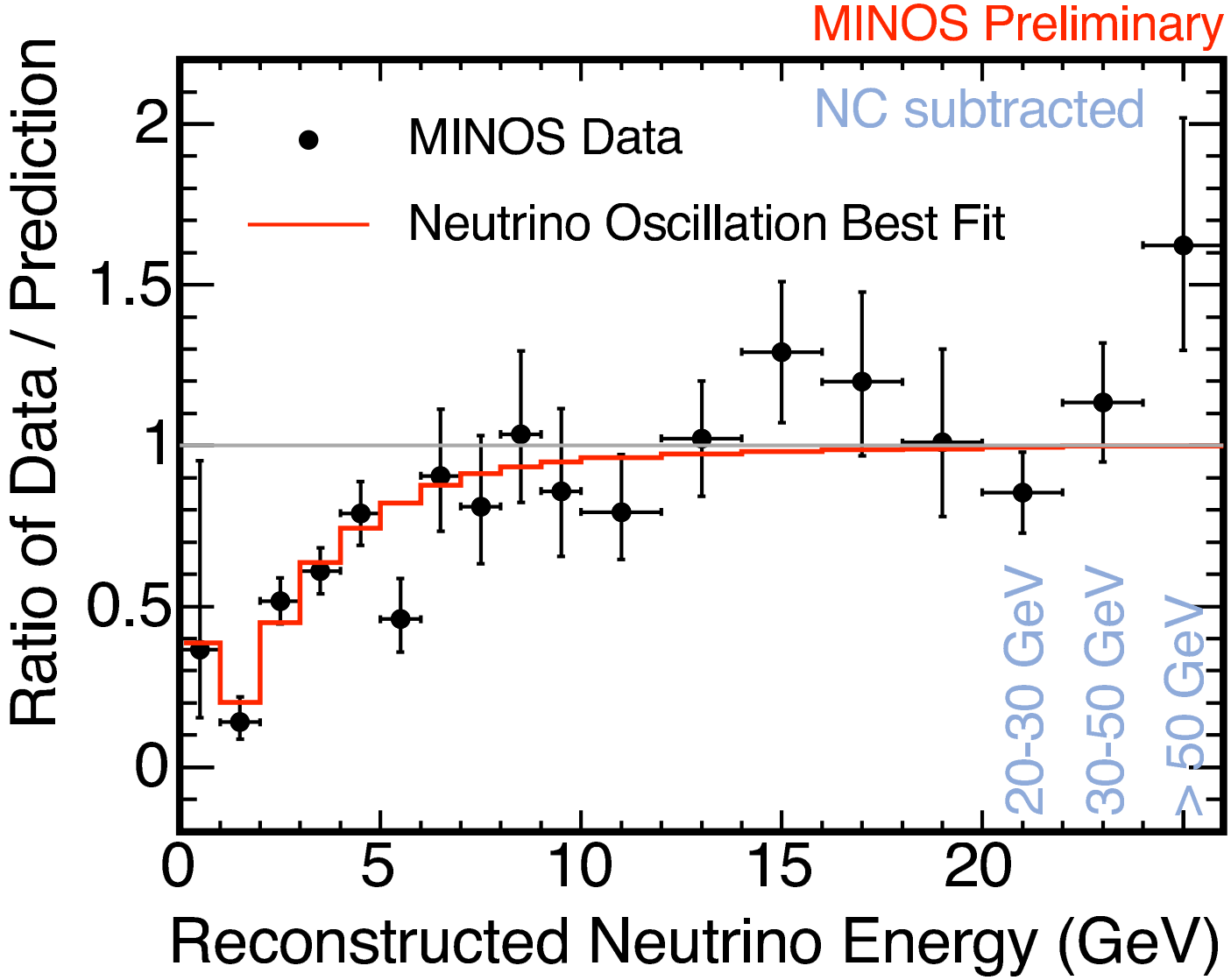
$$P_{\alpha\to\beta} = \sin^2 2\theta \sin^2\left(\Delta m^2 L/4E\right)$$

SuperK Atmospheric Neutrinos



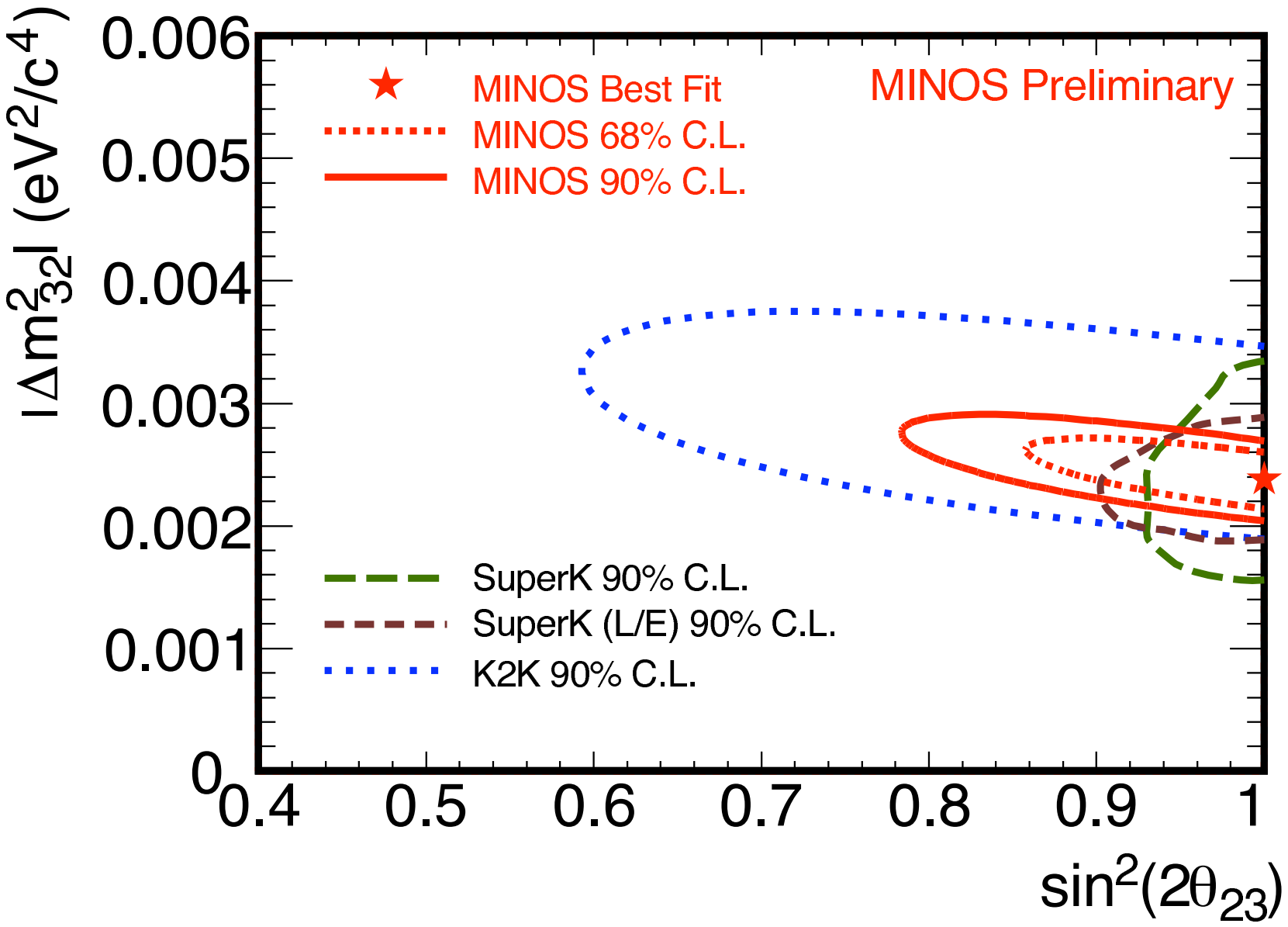
Downward ν travel 15 km, upward ν up to 13 000 km

MINOS ν_μ Deficit

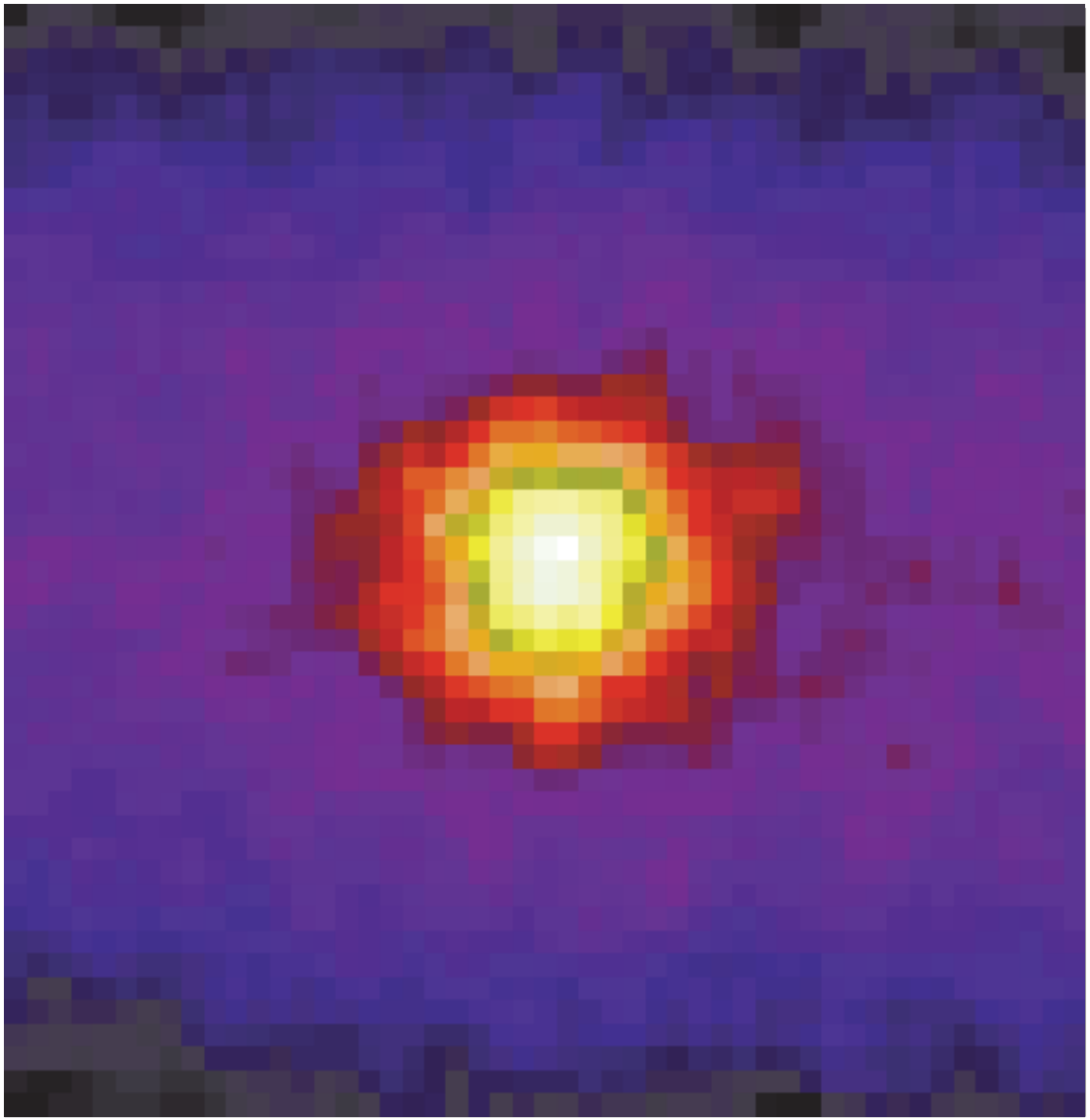


arXiv:0708.1495 [hep-ex]

Atmospheric Neutrino Summary



SuperK All-Sky Map in Neutrinos ($\nu e \to \nu e$)



$$4p \to {}^4\mathrm{He} + 2e^+ + 2\nu_e + 25\ \mathrm{MeV}$$

Solar neutrinos: measure three reaction rates

[CC] Charged-current dissociation: sensitive to ν_e flux

$$\nu_e \mathrm{d} \to e^- \; p \; p \quad W\text{-exchange}$$

[NC] Neutral-current dissociation: sensitive to total ν flux

$$\nu_\ell \mathrm{d} \to \nu_\ell \; p \; n \quad Z\text{-exchange}$$

[ES] Elastic scattering: sensitive to $\approx \nu_e + \frac{1}{7}(\nu_\mu + \nu_\tau)$ flux

$$\sigma(\nu_{\mu,\tau} e \to \nu_{\mu,\tau} e) = \frac{G_F^2 m_e E_\nu}{2\pi}\left[L_e^2 + R_e^2/3\right] \quad Z\text{-exchange}$$

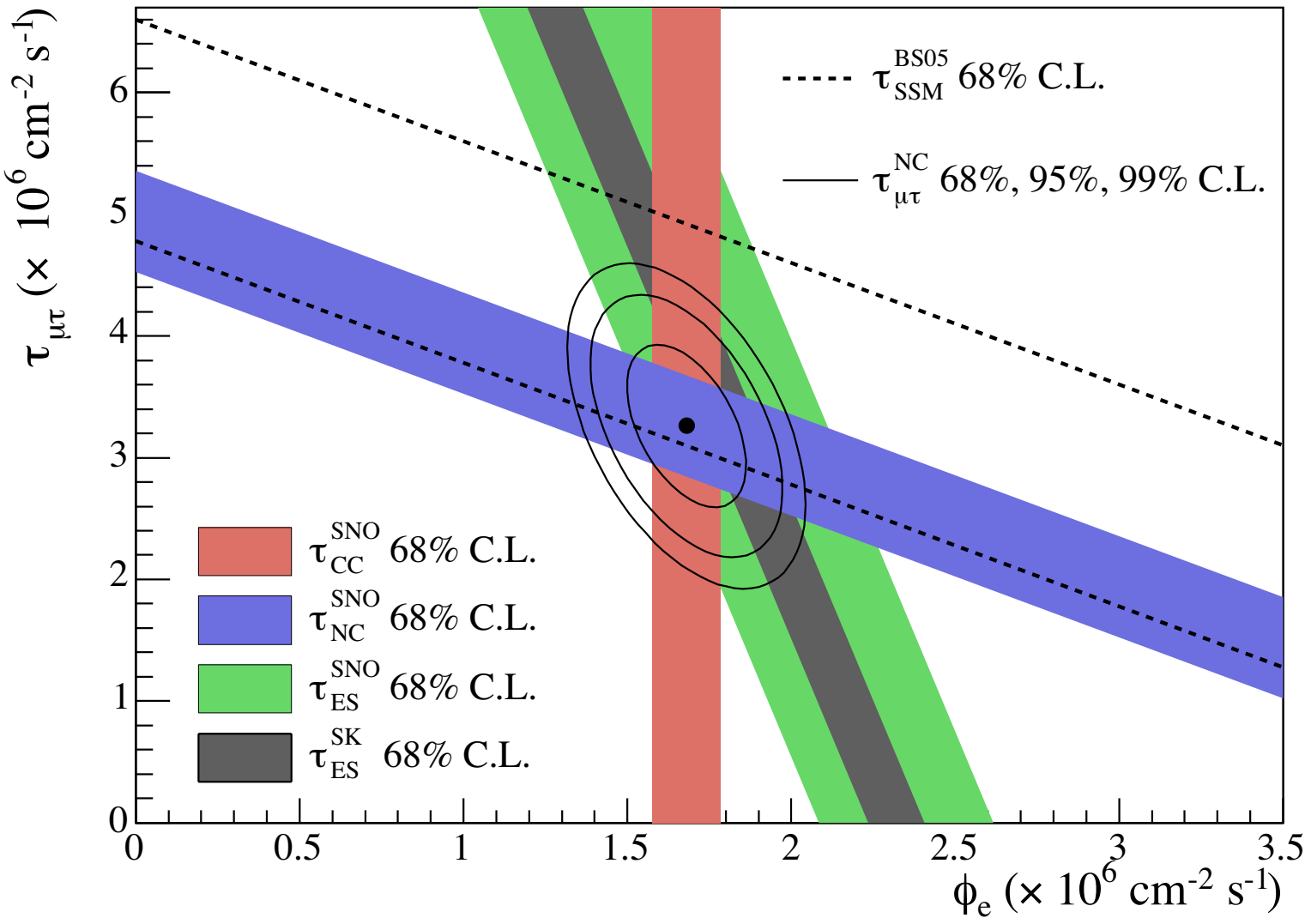
$$\sigma(\nu_e e \to \nu_e e) = \frac{G_F^2 m_e E_\nu}{2\pi}\left[(L_e+2)^2 + R_e^2/3\right] \quad W + Z\text{-exchange}$$

$$L_\ell = 2\sin^2\theta_W - 1 \approx -\tfrac{1}{2};\; R_\ell = 2\sin^2\theta_W \approx \tfrac{1}{2}$$

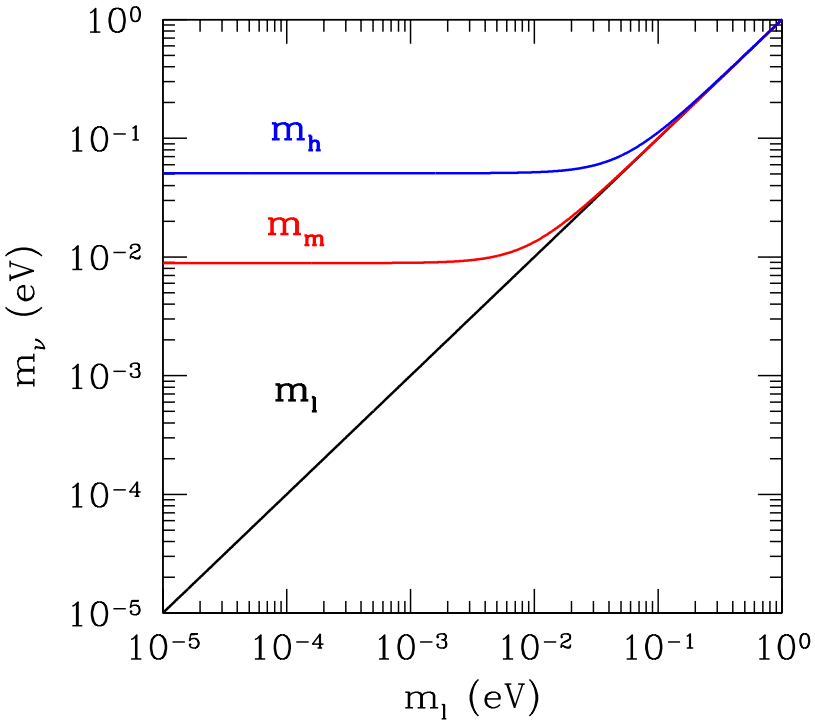
Solar neutrino observations: SuperK & SNO

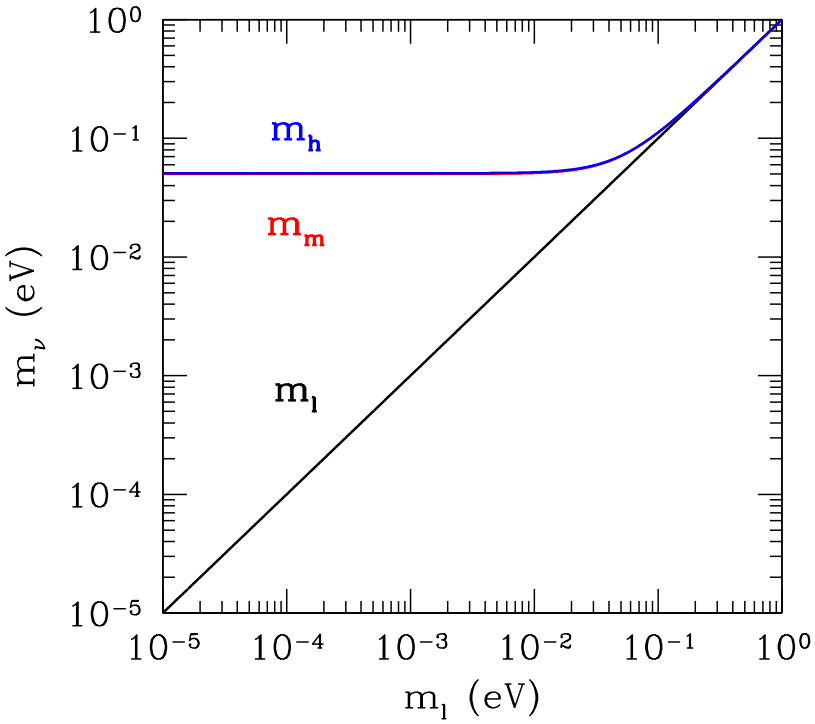
Total flux agrees with solar model, but only 30% arrive as ν_e

Solar ν emerge as ν_2



Absolute scale of neutrino masses is not yet known





Normal spectrum

Inverted spectrum

$$m_2^2 - m_1^2 = \Delta m_\odot^2 = 7.9 \times 10^{-5}\ \text{eV}^2 \qquad |m_3^2 - m_1^2| = \Delta m_{\text{atm}}^2 = 2.5 \times 10^{-3}\ \text{eV}^2$$

$$\rho_c \equiv 3H_0^2/8\pi G_N = 1.05h^2 \times 10^4\ \text{eV cm}^{-3} = 5.6 \times 10^3\ \text{eV cm}^{-3}$$

$$\boxed{(56\nu_i + 56\bar{\nu}_i)\ \text{cm}^{-3} \rightsquigarrow \sum_i m_{\nu_i} \lesssim 50\ \text{eV}}$$

Expectations for relic neutrinos

Relate to Cosmic Microwave Background:

$$\frac{dn_\gamma(T)}{d^3p} = \frac{1}{(2\pi)^3}\frac{1}{\exp(p/T)-1},$$

p: relic momentum, T: photon temperature

$$n_\gamma(T) = \frac{1}{(2\pi)^3}\int d^3p\,\frac{1}{\exp(p/T)-1} = \frac{2\zeta(3)}{\pi^2}\,T^3,$$

$T_0 = (2.725 \pm 0.002)$ K: $n_{\gamma 0} \equiv n_\gamma(T_0) \approx 410\ \mathrm{cm}^{-3}$

Expectations for relic neutrinos

ν decoupled around 1 MeV (0.1 s), were little reheated by e^+e^- annihilation: $T_\nu/T = \left(\frac{4}{11}\right)^{1/3}$ (below m_e).

$$T_{\nu 0} = \left(\tfrac{4}{11}\right)^{1/3} T_0 = 1.945 \text{ K} \rightsquigarrow 1.697 \times 10^{-4} \text{ eV} .$$

$$\frac{dn_{\nu_i}(T_\nu)}{d^3p} = \frac{1}{(2\pi)^3} \frac{1}{\exp\left(p/T_\nu\right) + 1} .$$

$$\begin{aligned} n_{\nu_i}(T_\nu) &= \frac{1}{(2\pi)^3} \int d^3p \, \frac{1}{\exp\left(p/T_\nu\right) + 1} \\ &= \frac{3\zeta(3)}{4\pi^2} T_\nu^3 = \tfrac{3}{22} n_\gamma(T) . \end{aligned}$$

Expectations for relic neutrinos

In the present Universe,

$$n_{\nu_i 0} = n_{\nu_i^c 0} \equiv n_{\nu_i}(T_{\nu 0}) \approx 56 \text{ cm}^{-3}$$

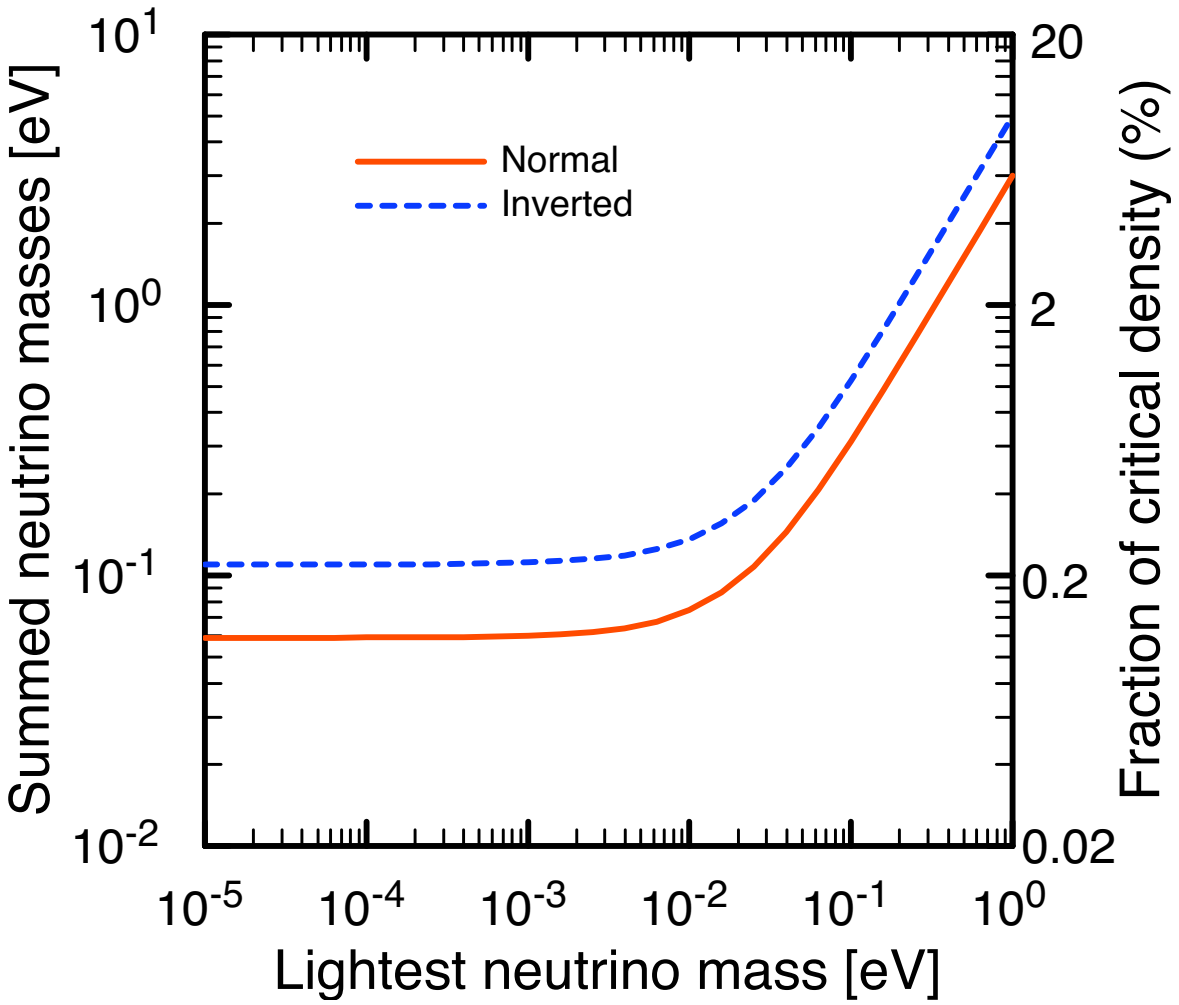
plus 1% from reheating ...

rms neutrino momentum:

$$\langle p_{\nu 0}^2 \rangle^{\frac{1}{2}} \approx 3.597\, T_{\nu 0} \approx 6.044 \times 10^{-4} \text{ eV}$$

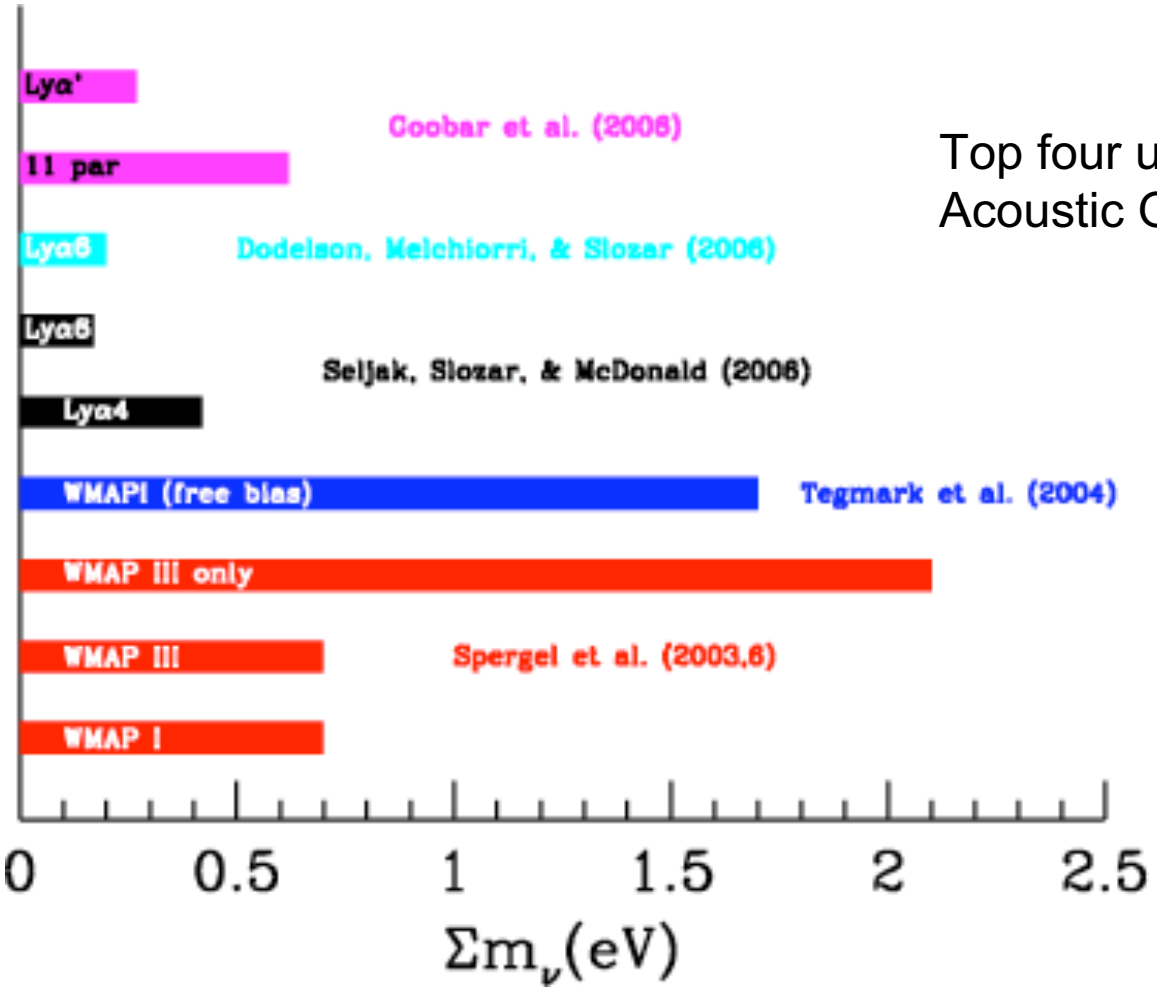
not necessarily small on scale of m_ν

$\sum_i m_{\nu_i}$



$\Omega_\nu \gtrsim (1.2, 2.2) \times 10^{-3}$ for (normal, inverted) spectrum

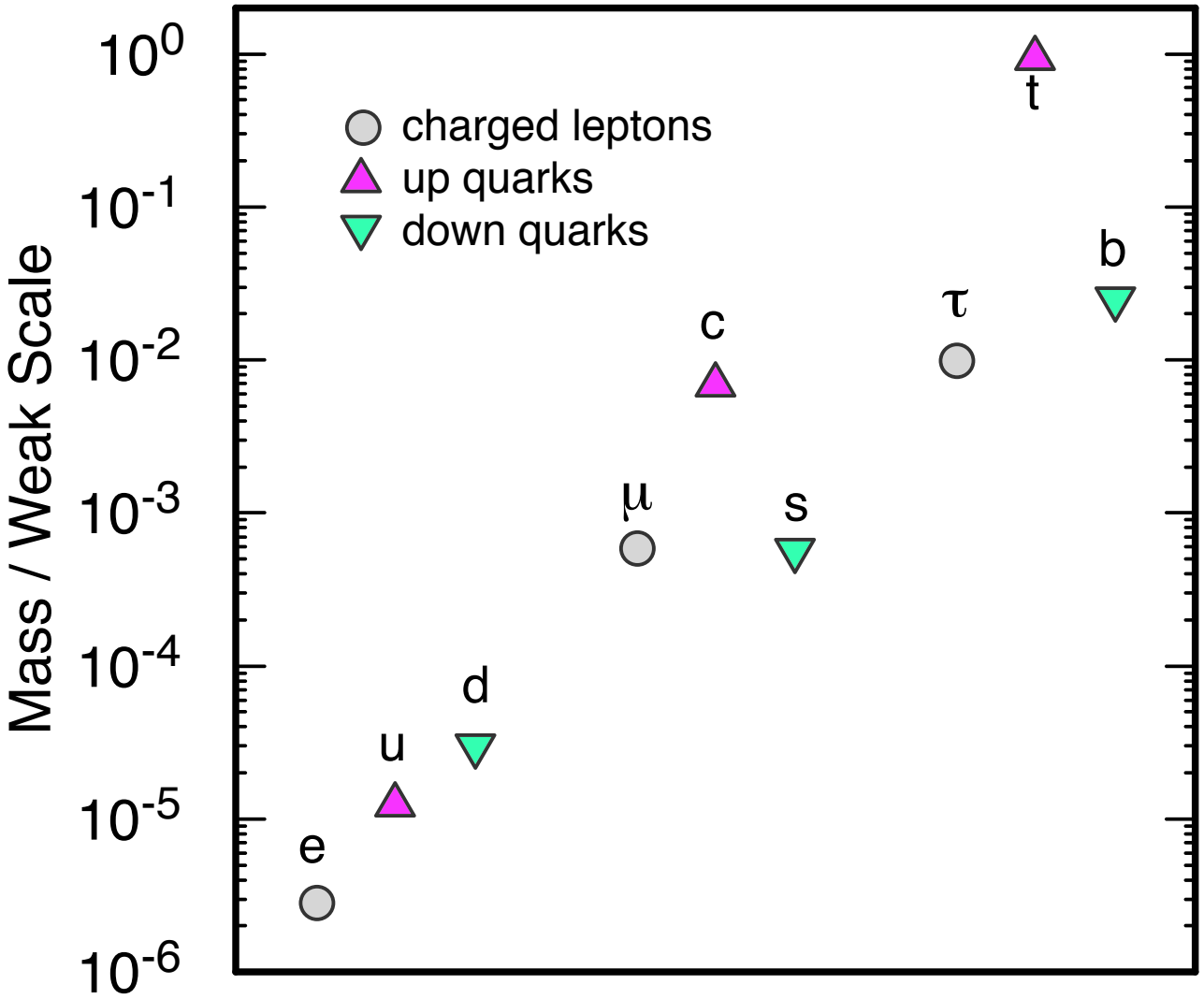
$\sum_i m_{\nu_i}$: cosmological constraints



Top four use Baryon Acoustic Oscillations

S. Dodelson, Fermilab–KEK ν School: http://nuss.fnal.gov

Quark & charged-lepton masses



If neutrinos have Dirac masses, ν Yukawa couplings $\lesssim 10^{-11}$

Summary of ν mixing parameters

Define $\boldsymbol{\nu} = (\nu_1, \nu_2, \nu_3) \quad \boldsymbol{\ell}_{\mathsf{L}} = (e_{\mathsf{L}}, \mu_{\mathsf{L}}, \tau_{\mathsf{L}})$

$$\mathcal{L}_{\mathsf{CC}}^{(q)} = -\frac{g}{\sqrt{2}} \bar{\boldsymbol{\nu}} \gamma^{\mu} \mathcal{V}^{\dagger} \boldsymbol{\ell}_{\mathsf{L}} W_{\mu}^{+} + \text{ h.c. },$$

$\mathcal{V}$: ν mixing matrix

$$\mathcal{V} = \begin{pmatrix} \mathcal{V}_{e1} & \mathcal{V}_{e2} & \mathcal{V}_{e3} \\ \mathcal{V}_{\mu 1} & \mathcal{V}_{\mu 2} & \mathcal{V}_{\mu 3} \\ \mathcal{V}_{\tau 1} & \mathcal{V}_{\tau 2} & \mathcal{V}_{\tau 3} \end{pmatrix}$$

Convention: ν_1, ν_2: solar pair, $m_1 < m_2$
ν_3 separated by Δm^2_{atm}; above or below?

Experiment tells us . . .

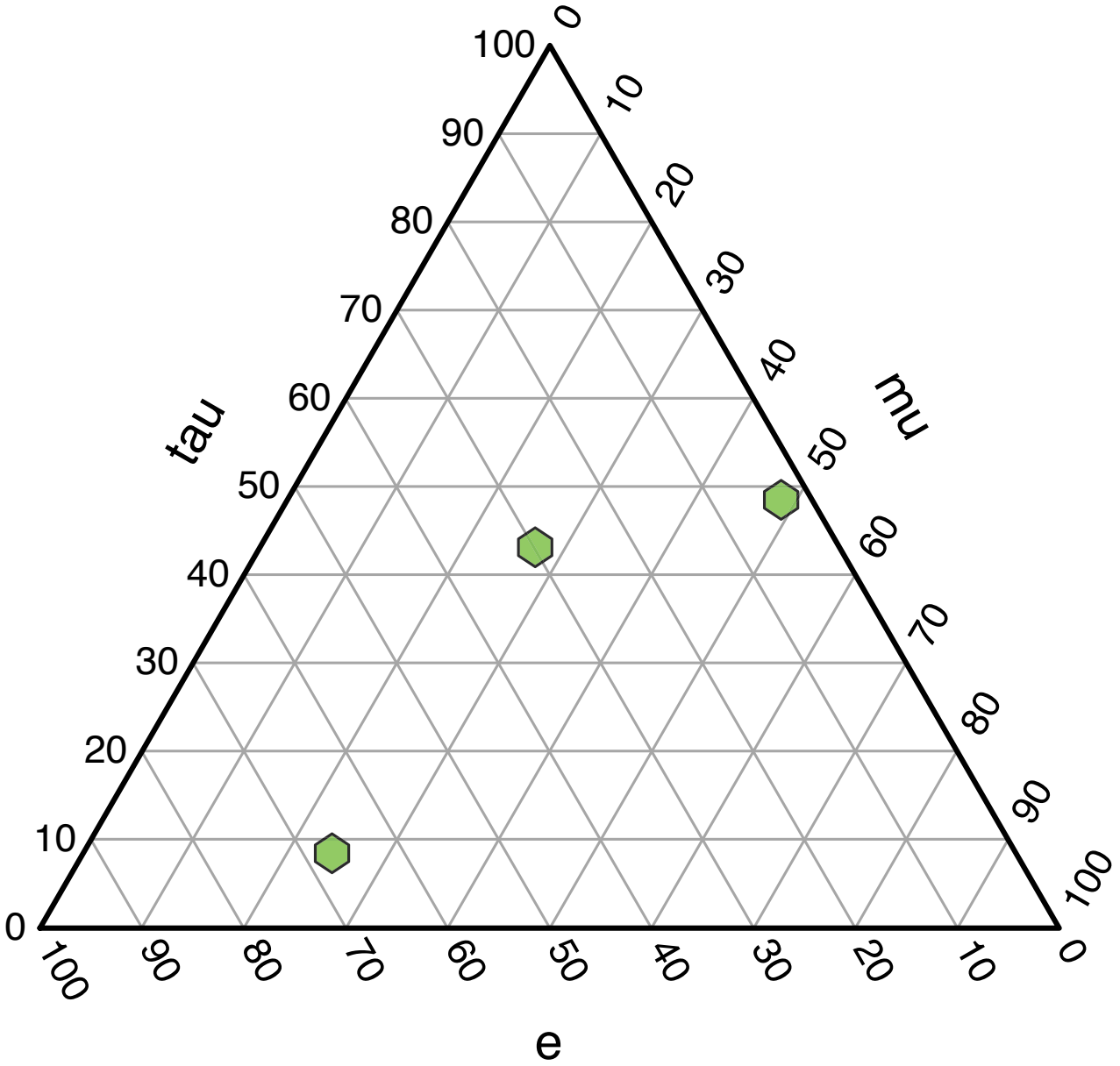
$$|\mathcal{V}| = \begin{pmatrix} 0.79 - 0.88 & 0.47 - 0.61 & < 0.20 \\ 0.19 - 0.52 & 0.42 - 0.73 & 0.58 - 0.82 \\ 0.20 - 0.53 & 0.44 - 0.74 & 0.56 - 0.81 \end{pmatrix}$$

$$\mathcal{V} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

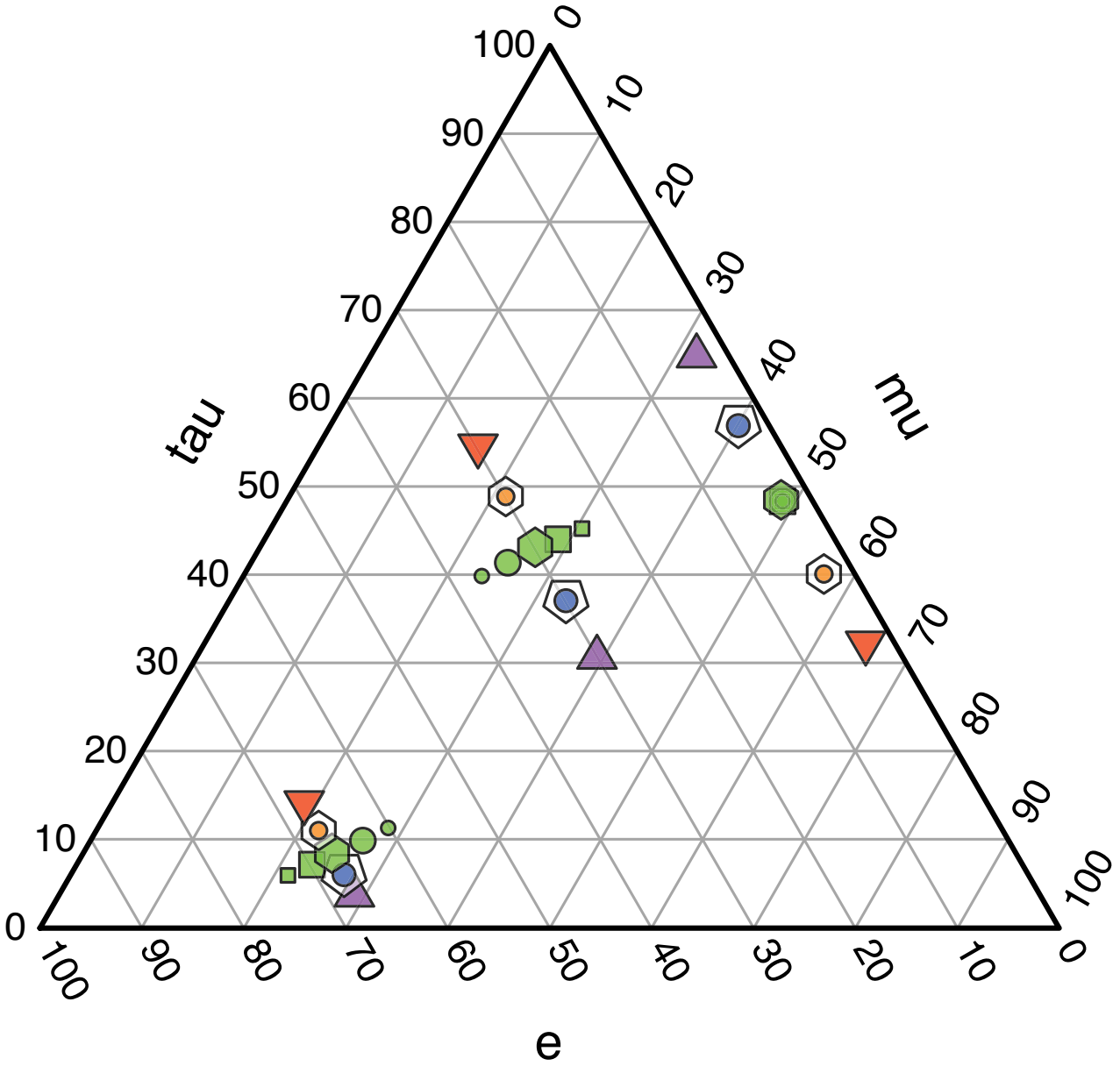
$s_{ij} = \sin\theta_{ij},\ c_{ij} = \cos\theta_{ij}$

$30^\circ \lesssim \theta_{12} \lesssim 38^\circ$: solar
$35^\circ \lesssim \theta_{23} \lesssim 55^\circ$: atm
$\theta_{13} \lesssim 10^\circ$
CP phase δ unconstrained

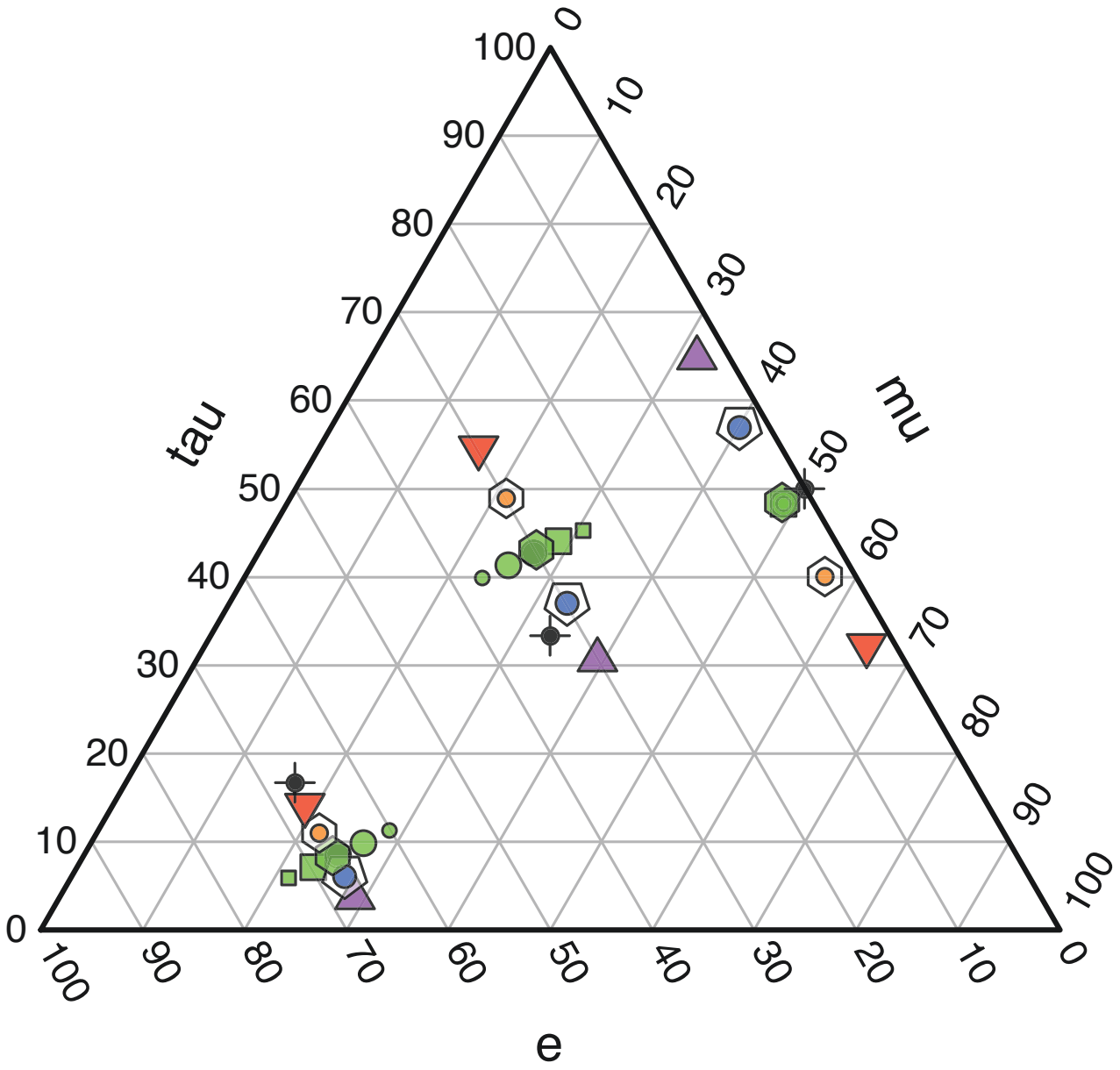
Neutrino Mixing (representative θ_{12}, θ_{23} values, $\theta_{13} = 10^\circ$)



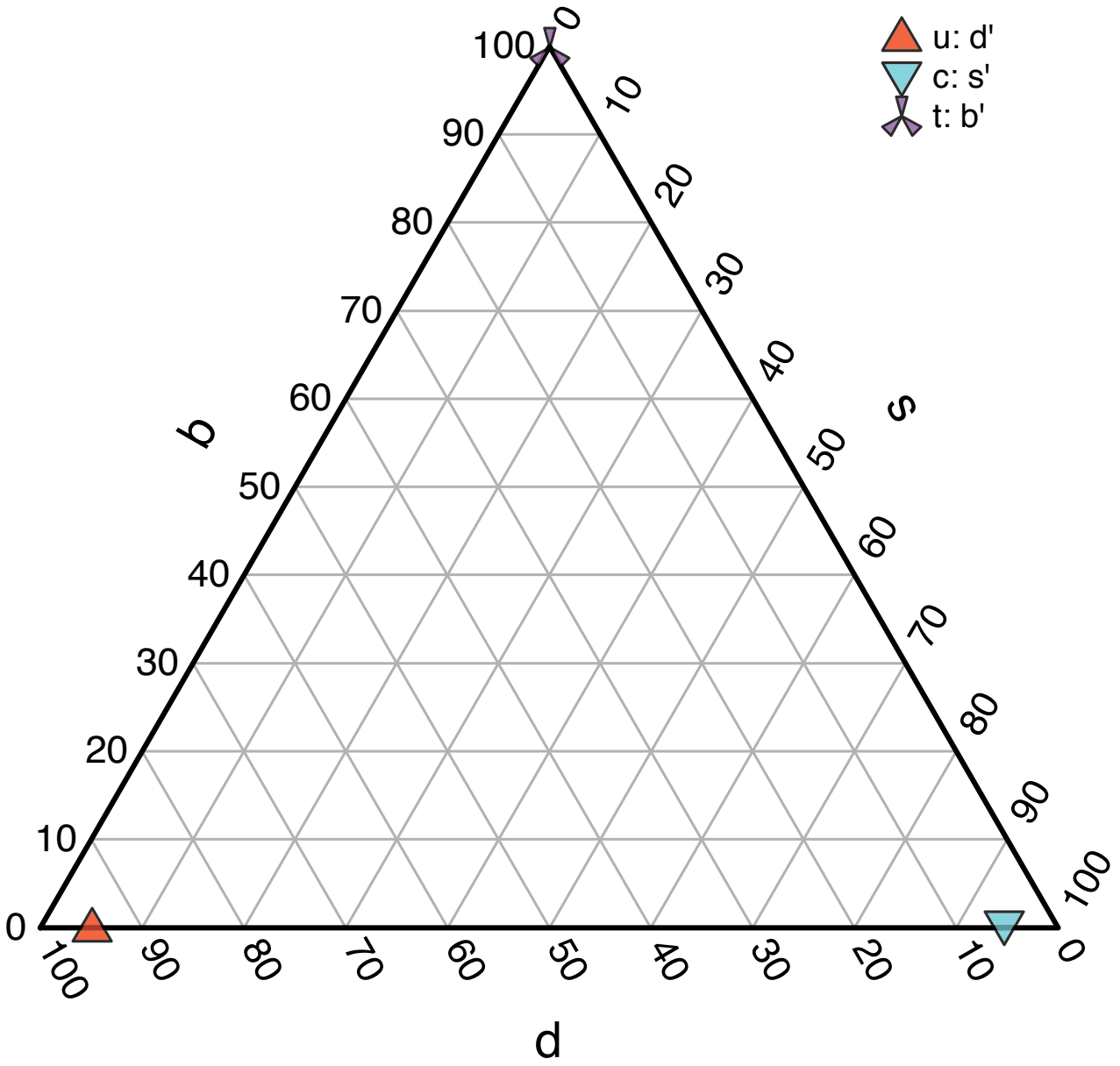
Neutrino Mixing (θ_{12}, θ_{23} variations, $\theta_{13} = 10^\circ$)



Neutrino Mixing (θ_{12}, θ_{23} variations, $\theta_{13} = 10^\circ$) TBM



Quark Mixing (Components: $|V_{u\alpha}|^2$, etc.)



Neutrino observatories: expectations

Cosmic ν flux may exceed atmospheric background at $E_\nu \approx$ few TeV

prospect for sources · characterize sources · study ν properties

Sources include AGN (at $\sim 10^2$ Mpc) 1 Mpc $\approx 3.1 \times 10^{22}$ m

pp or $p\gamma \Rightarrow$ $\approx$ numbers of π^+ π^0 π^-

$$\pi^+ + \pi^0 + \pi^- \Rightarrow 2\gamma + 2\nu_\mu + 2\bar{\nu}_\mu + 1\nu_e + 1\bar{\nu}_e$$

$$\boxed{\Phi^0_{\rm std} = \{\varphi^0_e = \tfrac{1}{3}, \varphi^0_\mu = \tfrac{2}{3}, \varphi^0_\tau = 0\} \quad (\nu = \bar{\nu})}$$

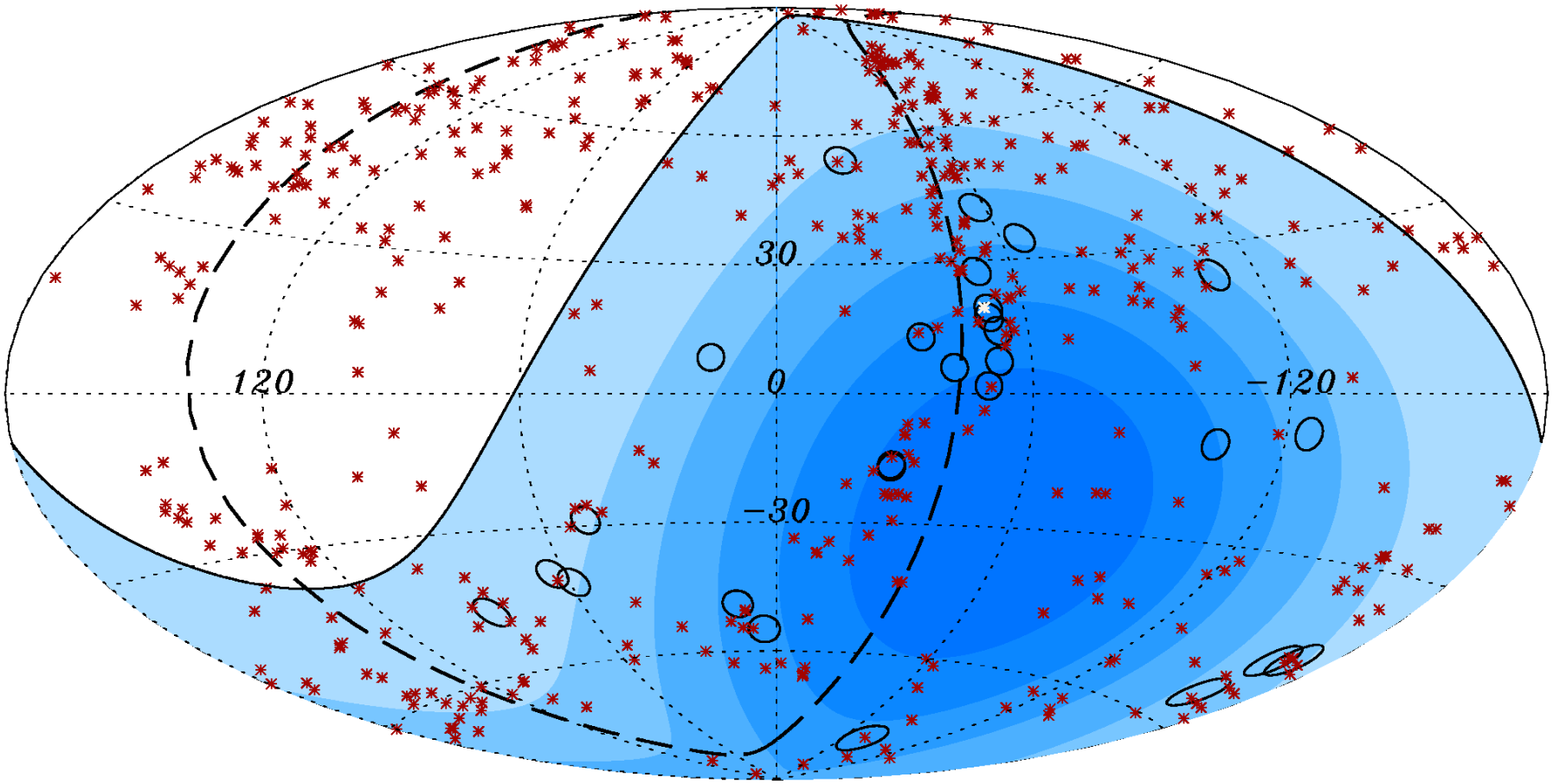
Detection (in volumes $\rightarrow 1$ km^3)

$$\boxed{(\nu_\mu, \bar{\nu}_\mu) N \rightarrow (\mu^-, \mu^+) + \text{anything}}$$

Can we achieve efficient, calibrated $(\nu_e, \bar{\nu}_e)$ detection?

Good $(\nu_\tau, \bar{\nu}_\tau)$ detection, NC capability desirable

Auger suggests AGN sources of highest-energy cosmic rays



arXiv:0711.2256

$\nu_\mu N \to \mu^- +$ anything

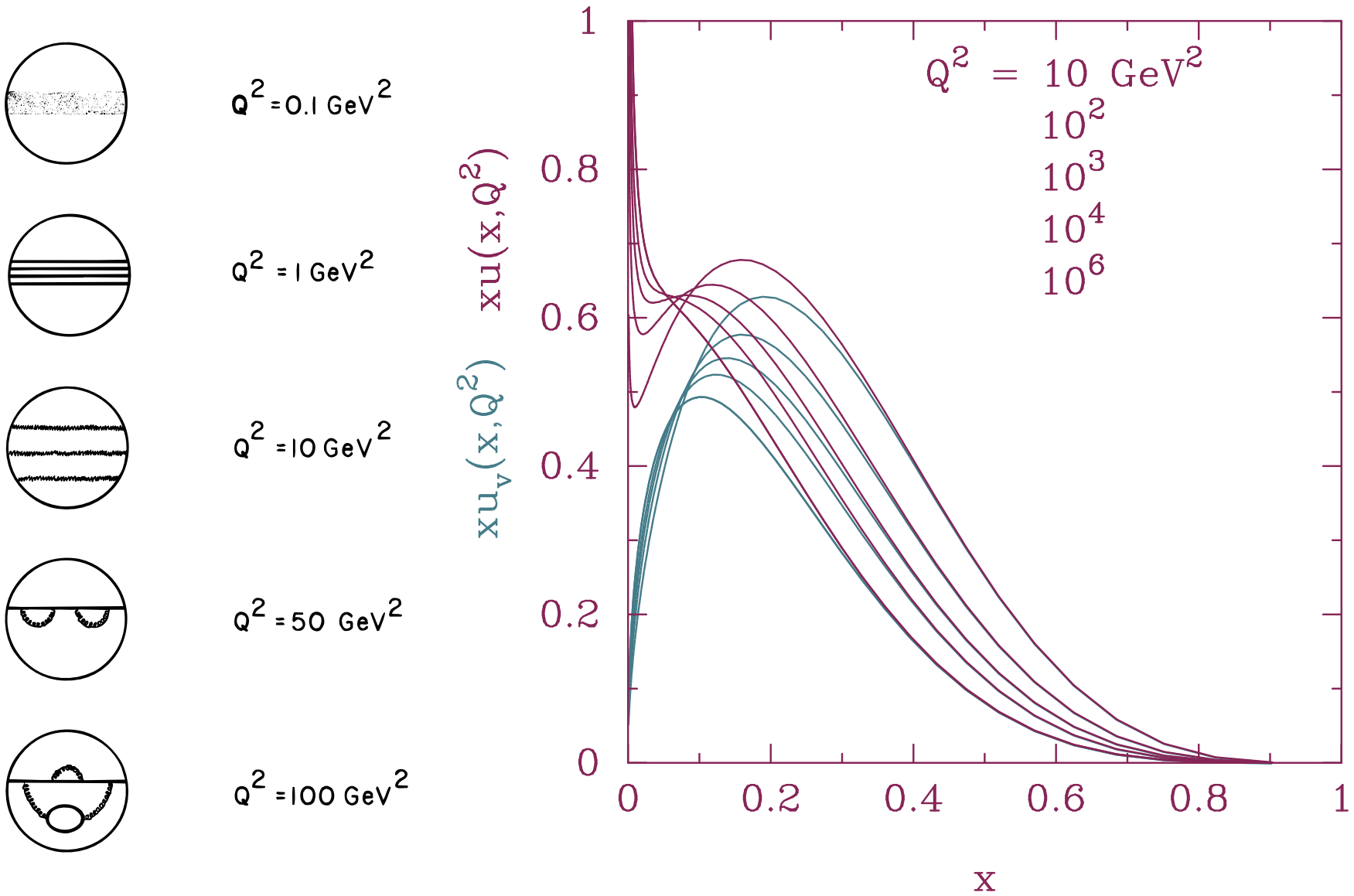
$$\frac{d^2\sigma}{dxdy} = \frac{2G_F^2 M E_\nu}{\pi}\left(\frac{M_W^2}{Q^2+M_W^2}\right)^2 \left[xq(x,Q^2) + x\bar{q}(x,Q^2)(1-y)^2\right]$$

$$\begin{aligned} q(x,Q^2) &= \frac{u_v(x,Q^2)+d_v(x,Q^2)}{2} + \frac{u_s(x,Q^2)+d_s(x,Q^2)}{2} \\ &\quad + s_s(x,Q^2) + b_s(x,Q^2) \\ \bar{q}(x,Q^2) &= \frac{u_s(x,Q^2)+d_s(x,Q^2)}{2} + c_s(x,Q^2) + t_s(x,Q^2), \end{aligned}$$

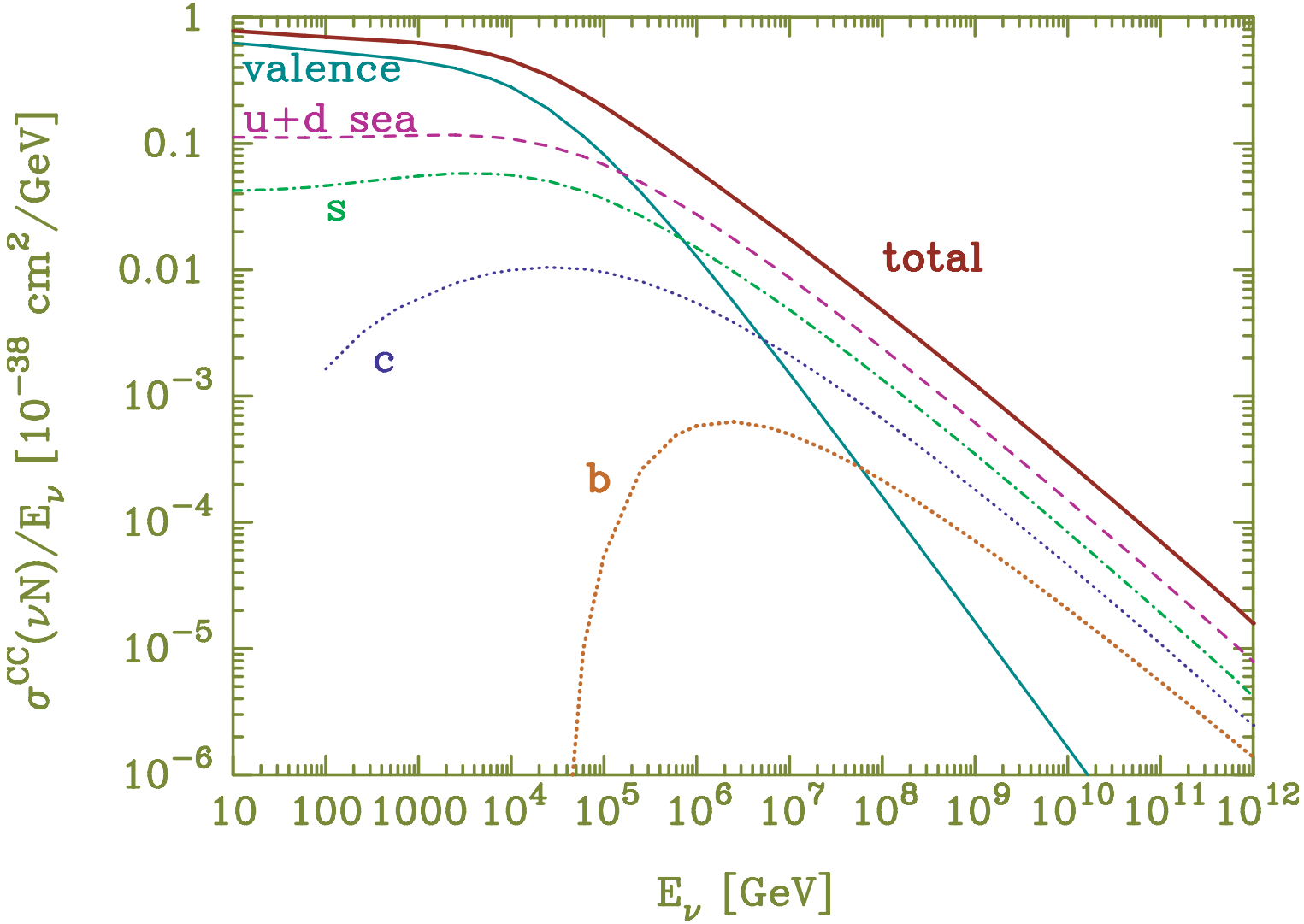
. . . isoscalar nucleon

$$x = Q^2/2M\nu \qquad y \equiv \nu/E_\nu \qquad \nu \equiv E_\nu - E_\mu$$

QCD Evolution of parton distributions . . .

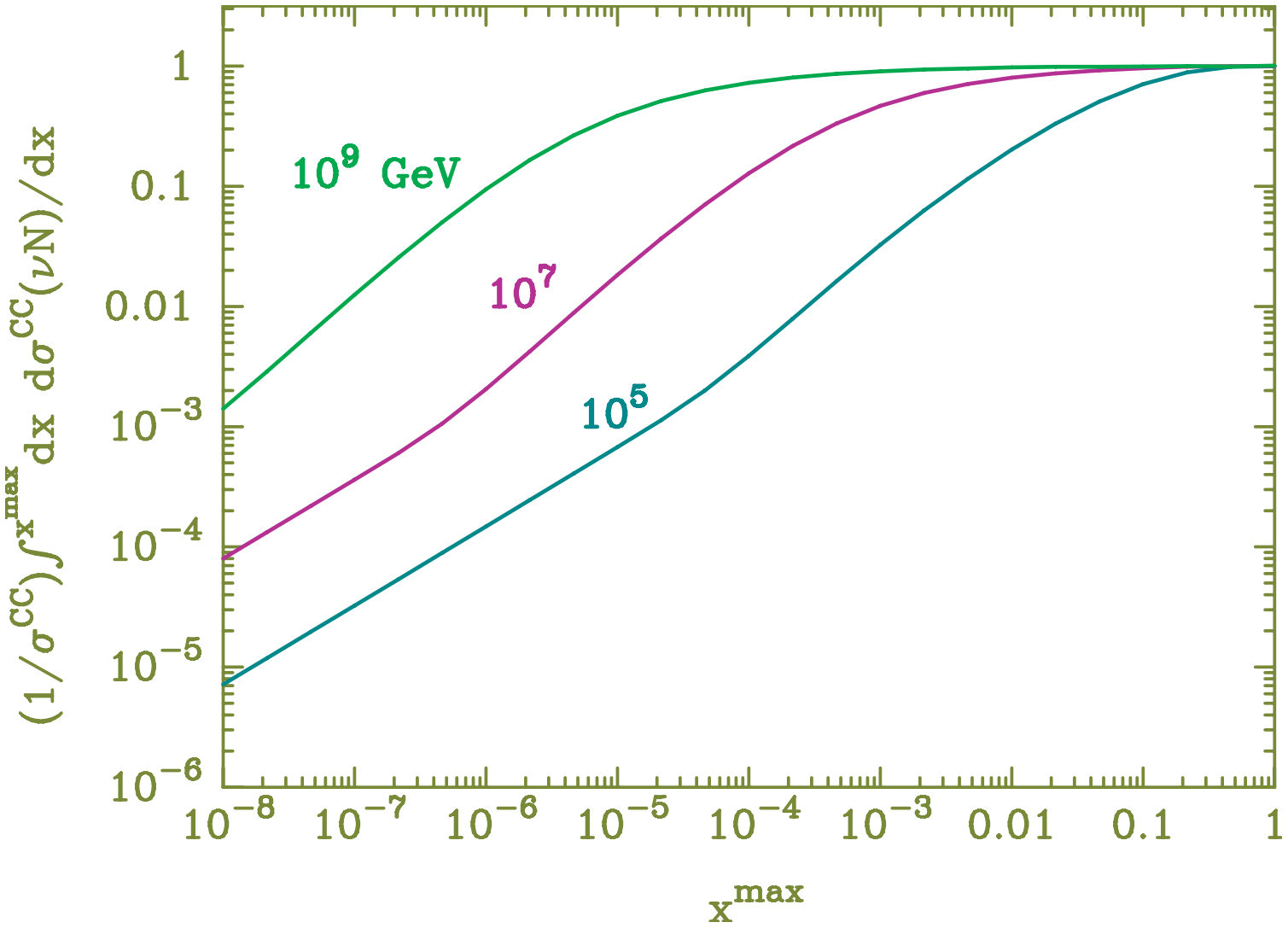


Components of σ_{CC}

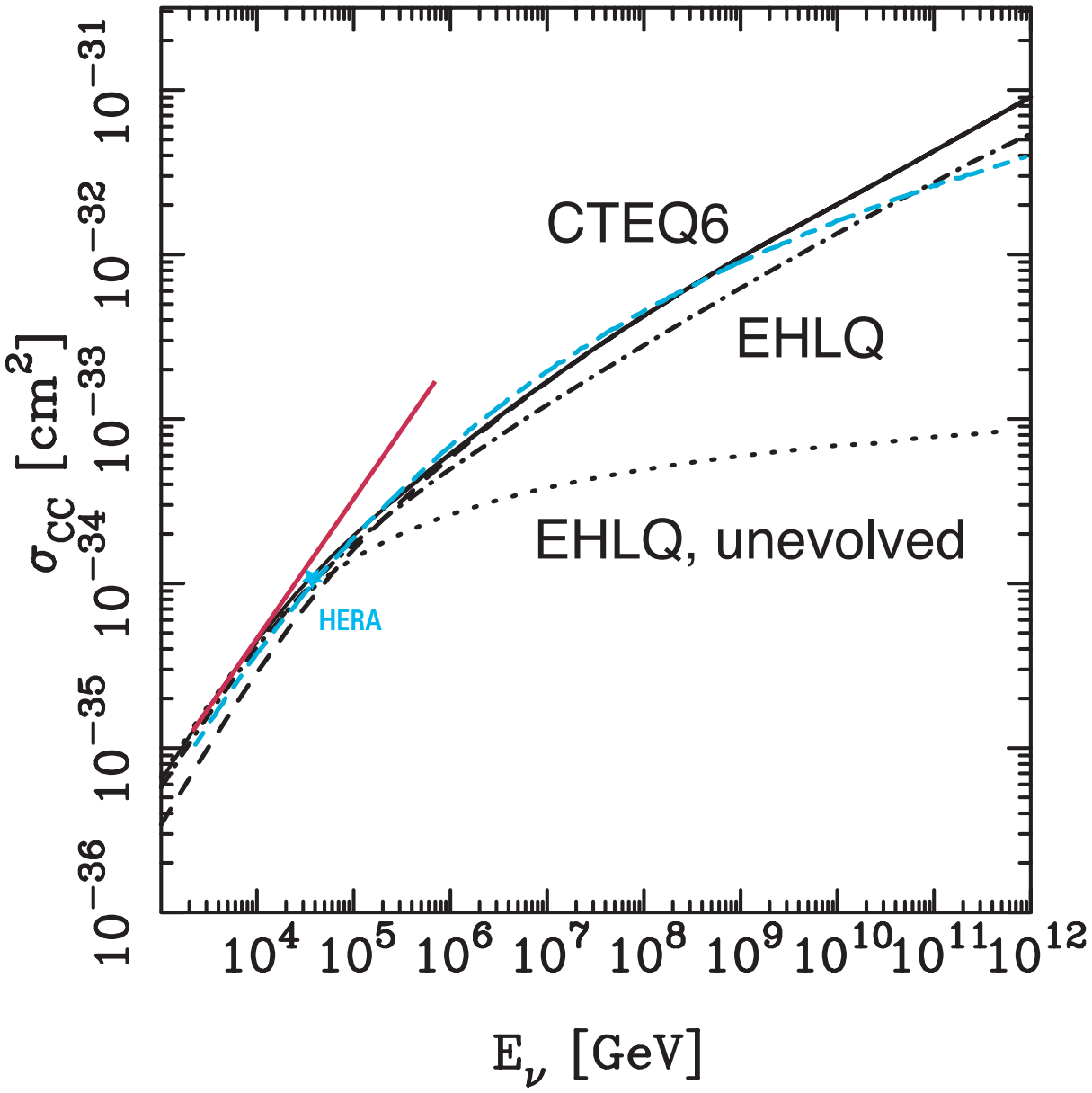


Gandhi, CQ, Reno, Sarcevic

Important regions of x at different E_ν

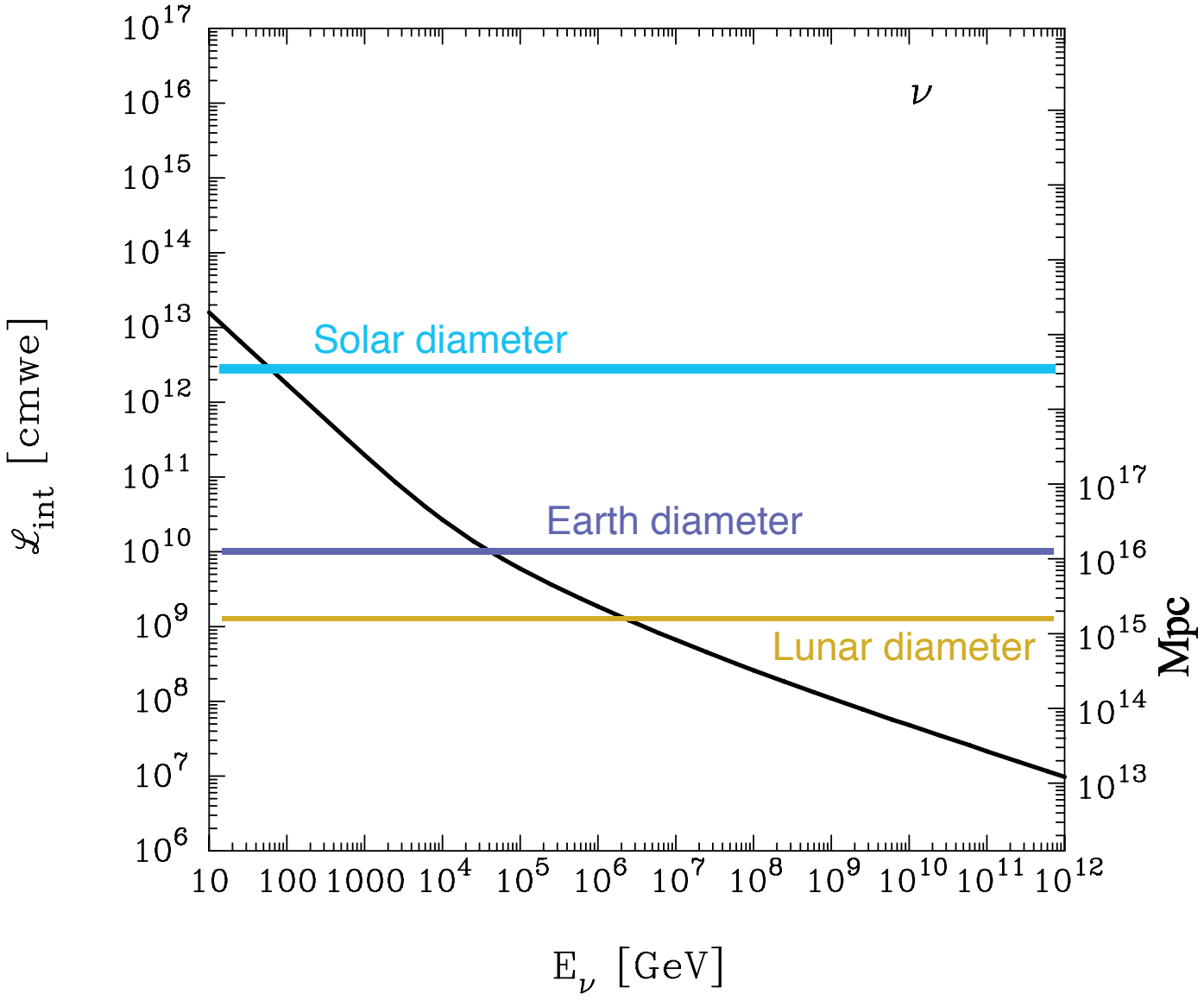


$\nu N \to \mu + \ldots$ Cross Sections



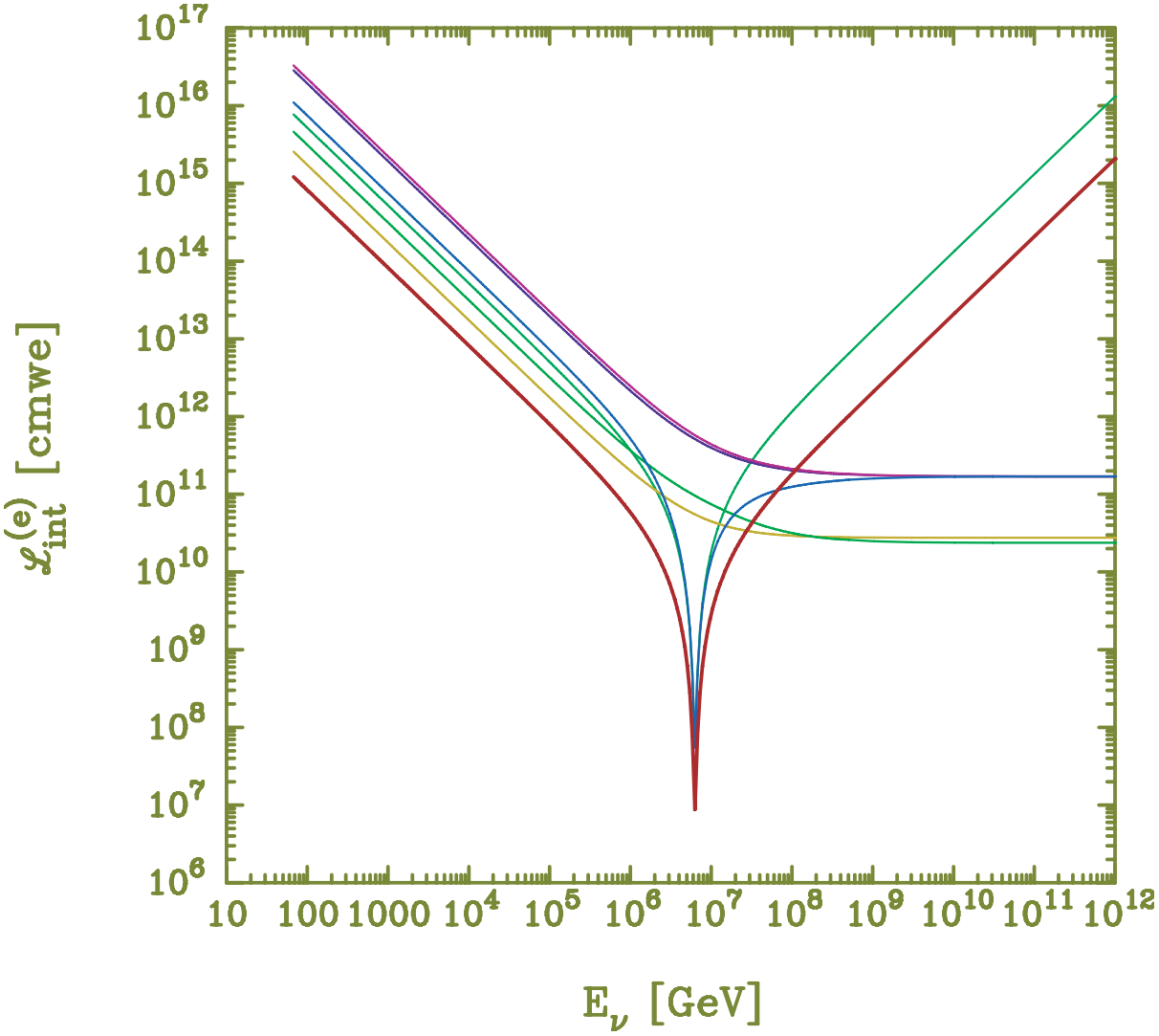
M. H. Reno

$\nu N \to \mu + \ldots$ interaction lengths



$n_{B0} \approx 2.5 \times 10^{-7}$ cm^{-3}

νe interaction lengths . . .

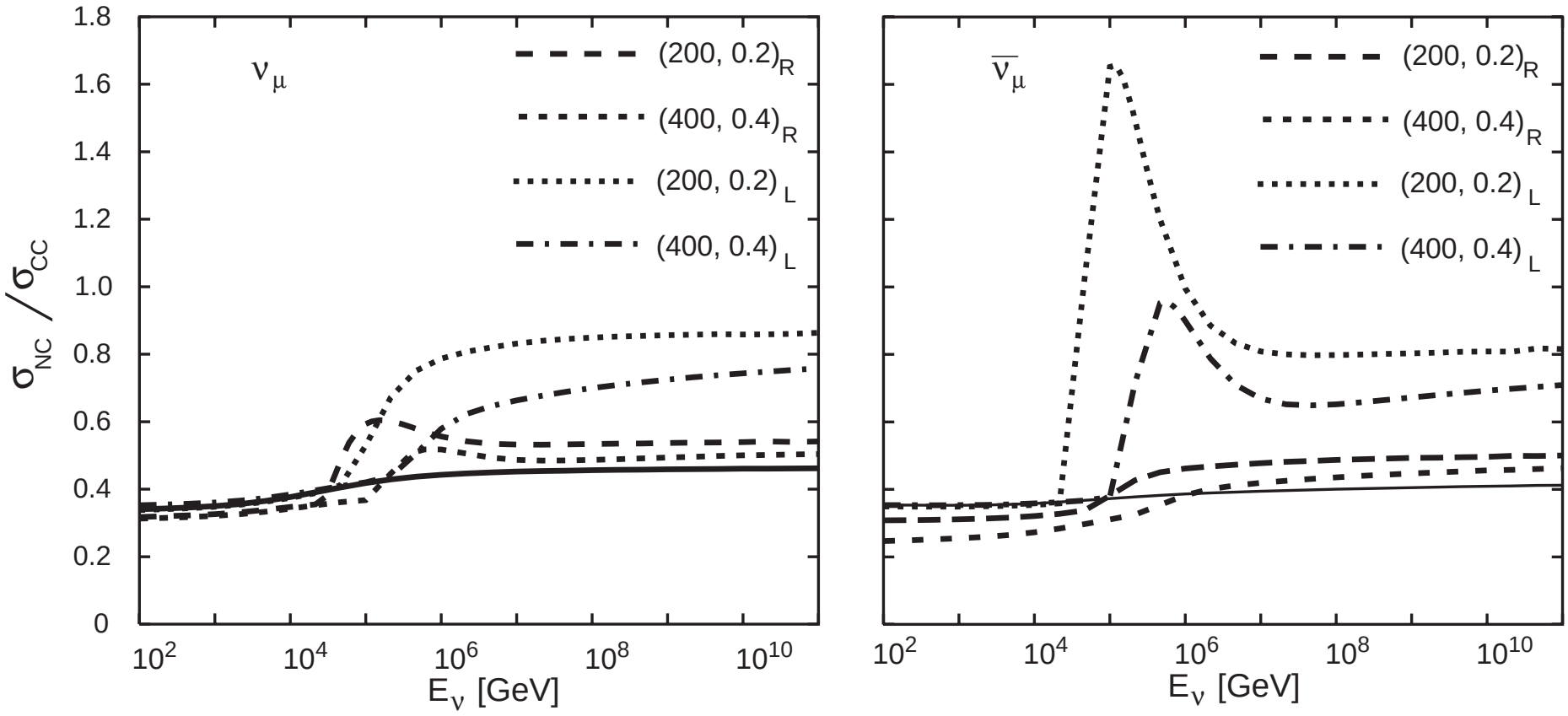


At low energies: $\mathcal{L}(\bar{\nu}_e e \to$ hadrons$) < \mathcal{L}(\nu_\mu e \to \mu\nu_e) < \mathcal{L}(\nu_e e \to \nu_e e) < \mathcal{L}(\bar{\nu}_e e \to \bar{\nu}_\mu \mu) < \mathcal{L}(\bar{\nu}_e e \to \bar{\nu}_e e) < \mathcal{L}(\nu_\mu e \to \nu_\mu e) < \mathcal{L}(\bar{\nu}_\mu e \to \bar{\nu}_\mu e)$

New Physics in νN interactions?

NC/CC an important diagnostic

$\tilde{d}^k_{\mathrm{L,R}}$ production through $\not{R}$ interactions: $(\tilde{m}, \lambda')$



Carena, Choudhury, Lola, CQ

Influence of neutrino oscillations

Flux at Earth $\Phi = \{\varphi_e, \varphi_\mu, \varphi_\tau\} \neq \Phi^0 = \{\varphi_e^0, \varphi_\mu^0, \varphi_\tau^0\}$ source fluxes

Vacuum oscillation length is short; for $|\Delta m^2| = 10^{-5}$ eV^2,

$$L_{\rm osc} \;=\; 4\pi E_\nu/|\Delta m^2| \approx 2.5 \times 10^{-24}\ \text{Mpc} \cdot (E_\nu/1\ \text{eV})$$

...a fraction of Mpc even for $E_\nu = 10^{20}$ eV

ν oscillate many times between cosmic source and terrestrial detector

Also, over long paths, cosmic neutrinos are vulnerable to decay processes that would not affect terrestrial or solar experiments.

. . . Neutrino Oscillations

$$\text{(flavor)}\ \nu_\alpha = \sum_i \mathcal{V}_{\alpha i}\nu_i\ \text{(mass)}$$

Idealize $\sin\theta_{13} = 0$, $\sin 2\theta_{23} = 1$, write $x = \sin^2\theta_{12}\cos^2\theta_{12}$.

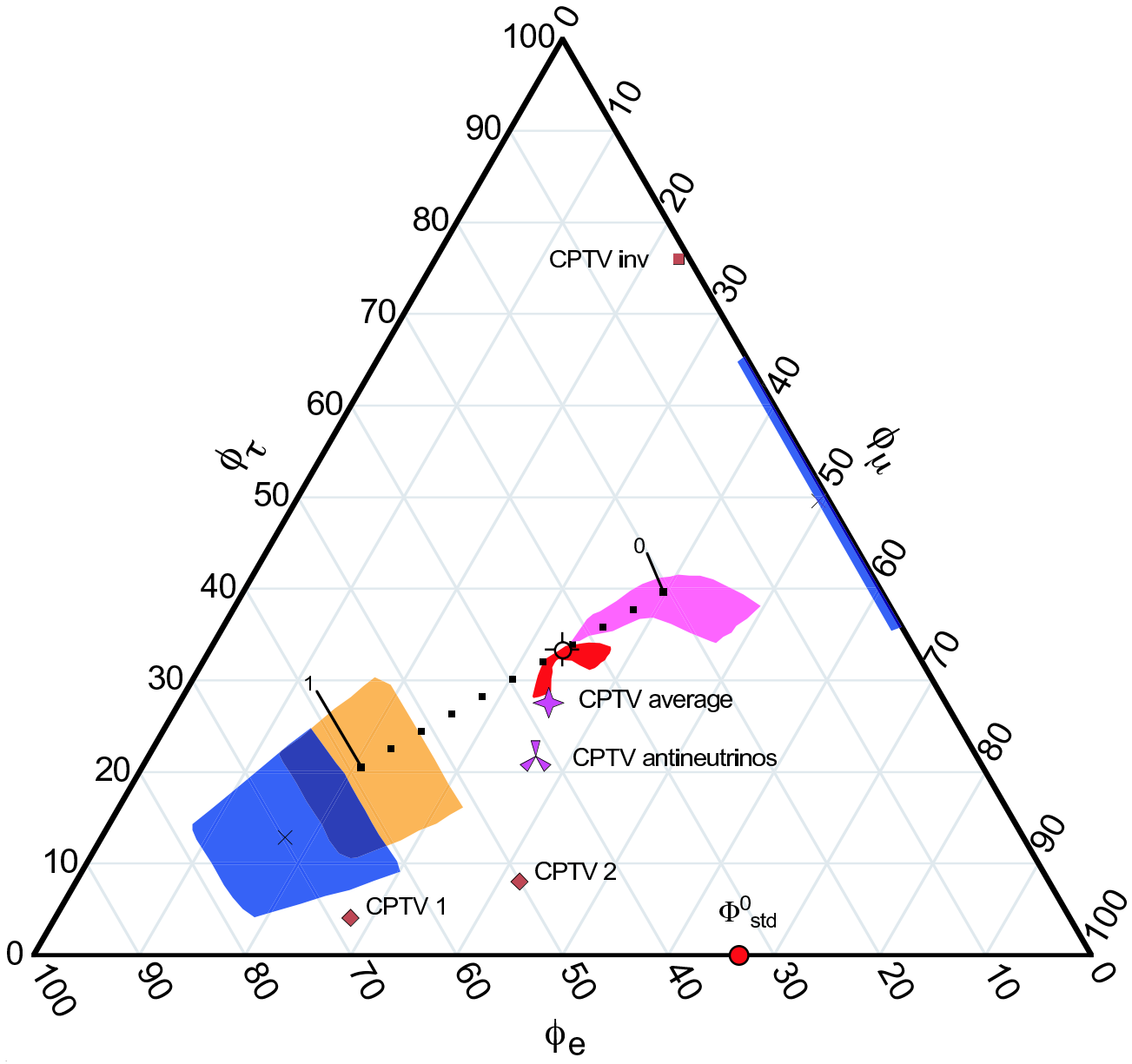
$$\mathcal{V}_{\text{ideal}} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12}/\sqrt{2} & c_{12}/\sqrt{2} & 1/\sqrt{2} \\ s_{12}/\sqrt{2} & -c_{12}/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}$$

Transfer matrix $\mathcal{X}$: Φ^0 (source) $\rightarrow \Phi$ (detector); Over many oscillations,

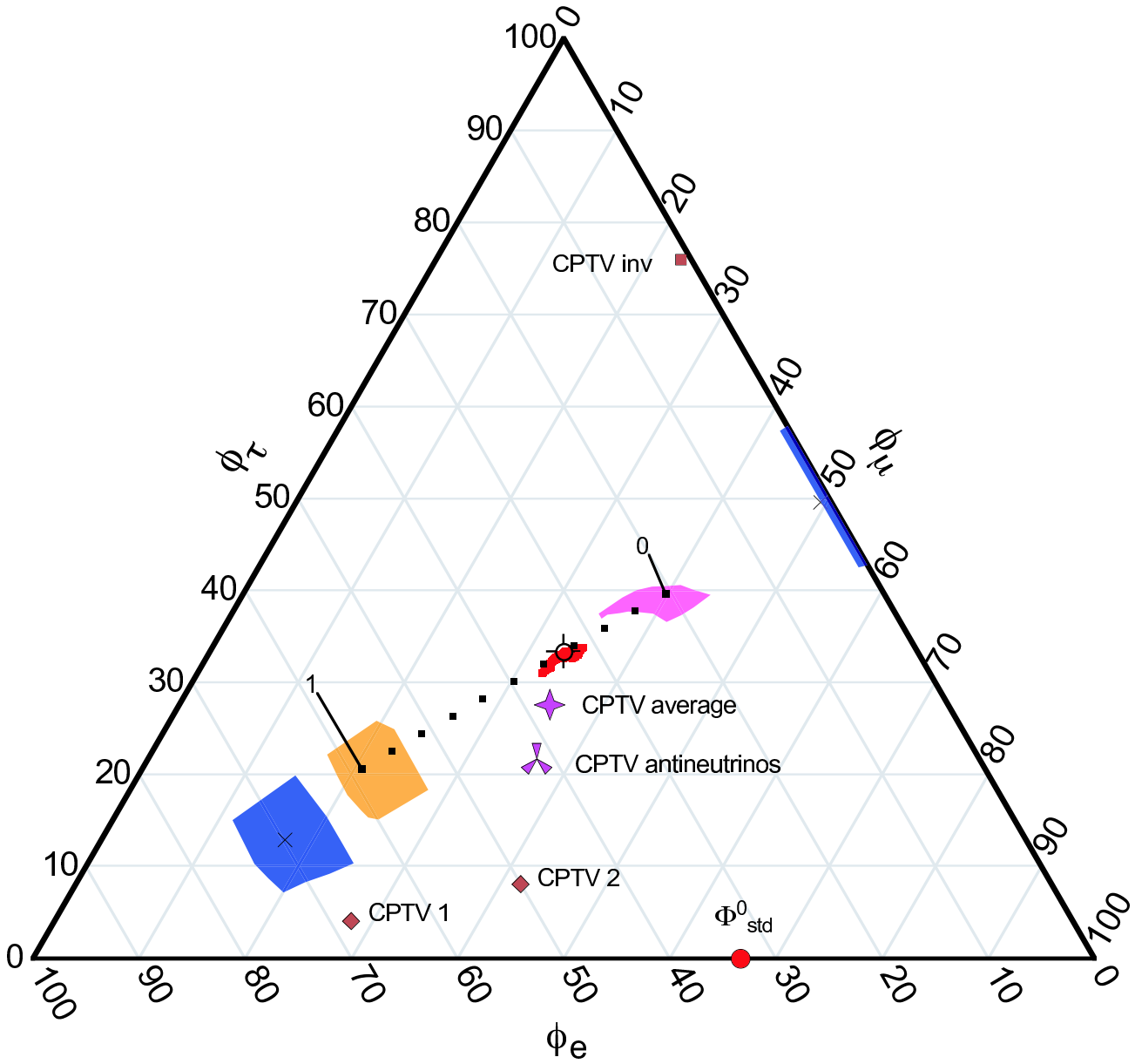
$$\mathcal{X}_{\text{ideal}} = \begin{pmatrix} 1-2x & x & x \\ x & \frac{1}{2}(1-x) & \frac{1}{2}(1-x) \\ x & \frac{1}{2}(1-x) & \frac{1}{2}(1-x) \end{pmatrix}$$

$$\boxed{\mathcal{X}_{\text{ideal}} : \Phi^0_{\text{std}} \rightarrow \{\varphi_e = \tfrac{1}{3}, \varphi_\mu = \tfrac{1}{3}, \varphi_\tau = \tfrac{1}{3}\}}$$

With current constraints . . .



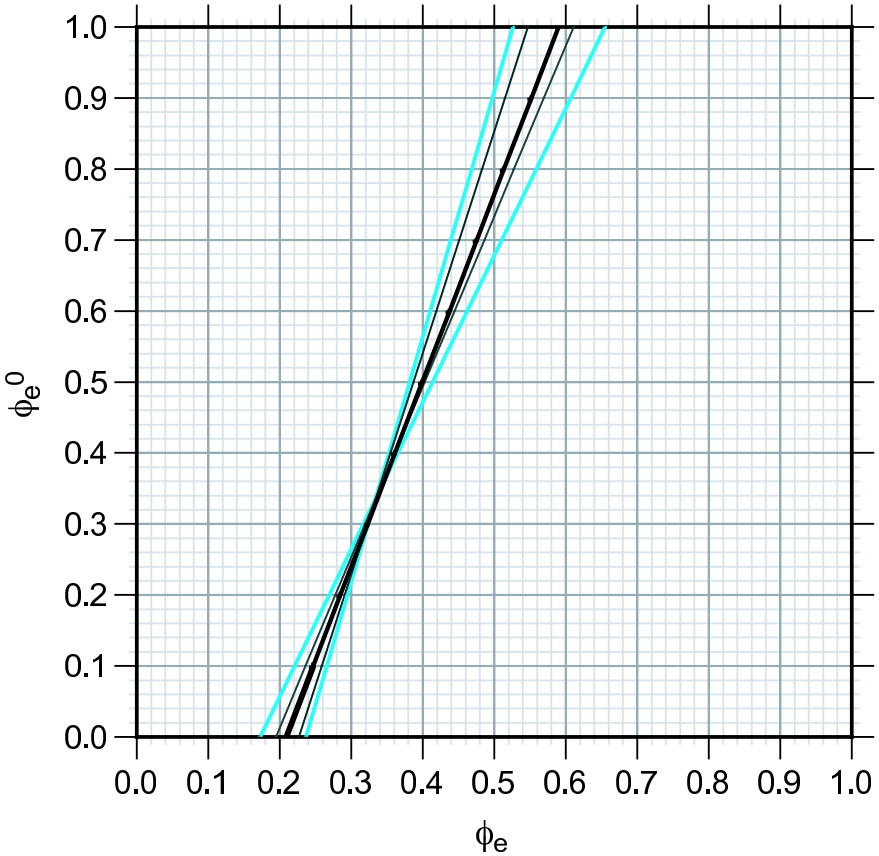
After current generation . . .



Reconstructing the ν Mixture at the Source

ν_μ, ν_τ fully mixed $\Rightarrow$ can't fully characterize Φ^0

Reconstruct ν_e fraction at source using $\mathcal{X}_{\rm ideal}$: $\varphi_e^0 = (\varphi_e - x)/(1-3x)$



Extreme φ_e implicates unconventional physics

Influence of neutrino decays

Nonradiative decays $\nu_i \to (\nu_j, \bar{\nu}_j) + X$ not very constrained:

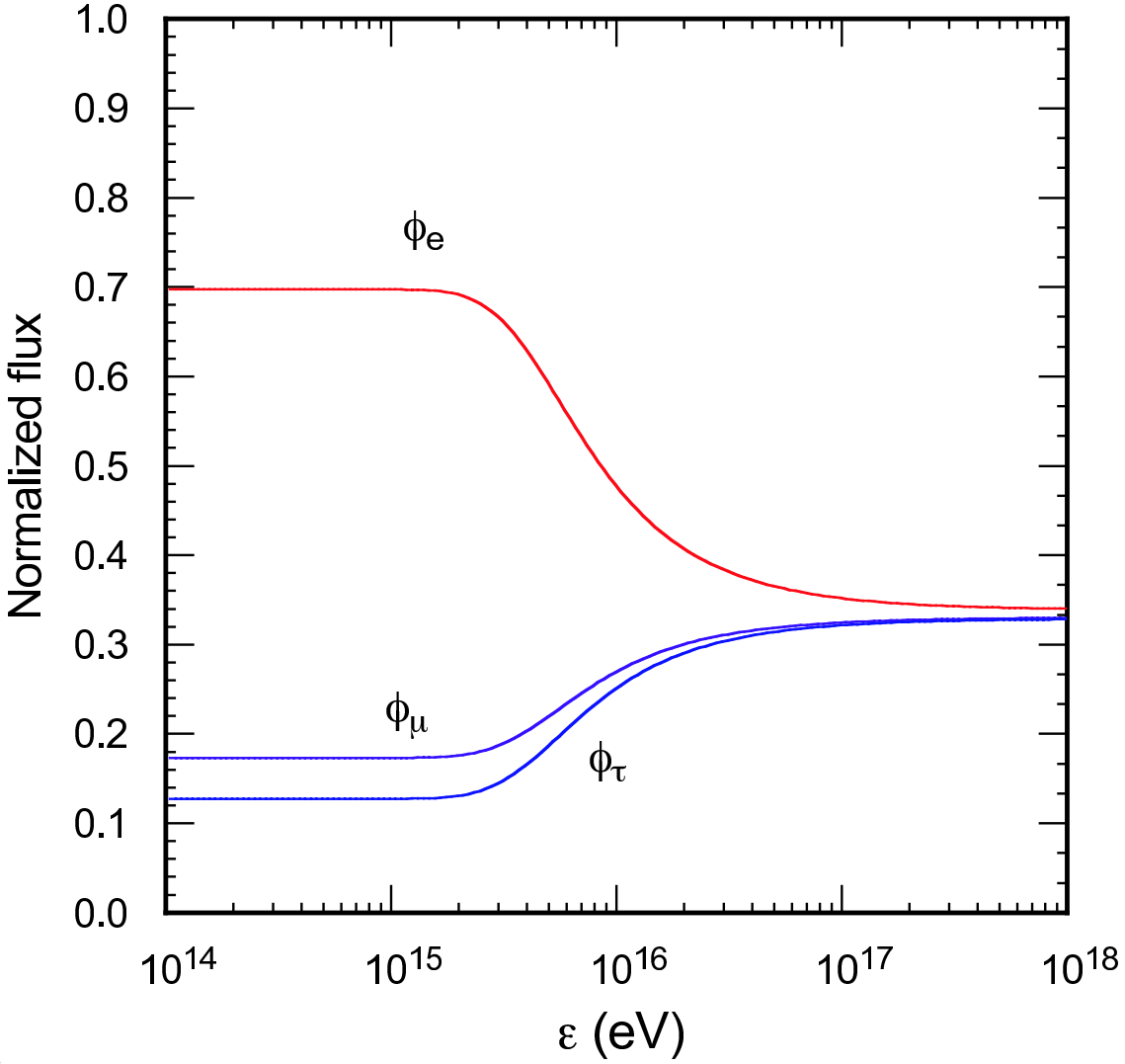
$$\tau/m \gtrsim 10^{-4}\ \mathrm{s/eV}$$

If only lightest neutrino survives, flavor mix at Earth is independent of composition at source

Normal hierarchy	Inverted hierarchy
$m_1 < m_2 < m_3$:	$m_1 > m_2 > m_3$:
$\varphi_\alpha = \lvert U_{\alpha 1}\rvert^2$	$\varphi_\alpha = \lvert U_{\alpha 3}\rvert^2$
$\Phi_{\text{normal}} \approx \{0.70, 0.17, 0.13\}$	$\Phi_{\text{inverted}} \approx \{0, 0.5, 0.5\}$

$$\boxed{\text{far from } \Phi_{\text{std}} = \{\tfrac{1}{3}, \tfrac{1}{3}, \tfrac{1}{3}\}}$$

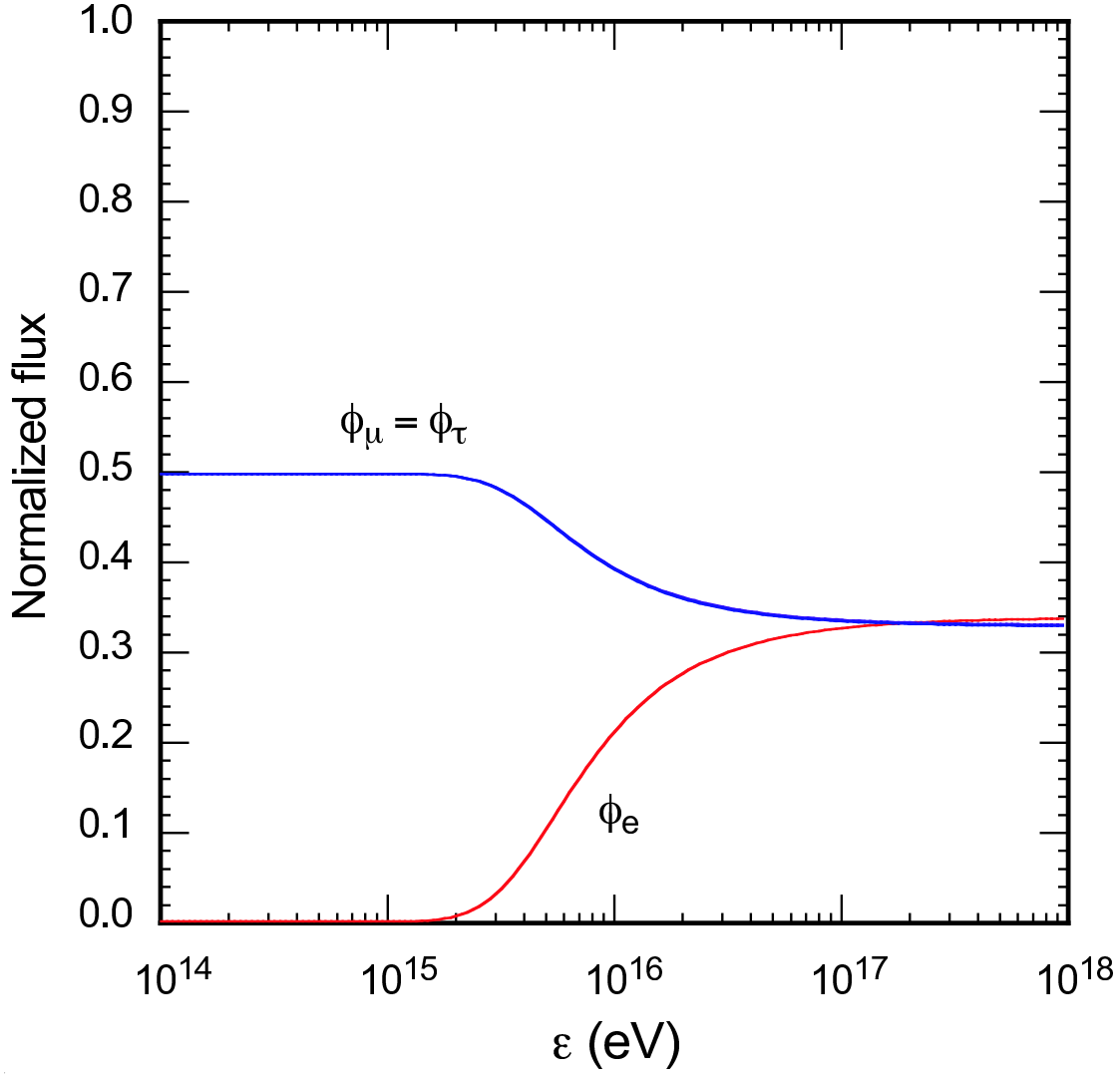
Energy-dependent composition as marker of ν decays



$E_\nu = \varepsilon(1\ \mathrm{s/eV})/(\tau_\nu/m_\nu) \cdot L/(100\ \mathrm{Mpc})$

Normal hierarchy

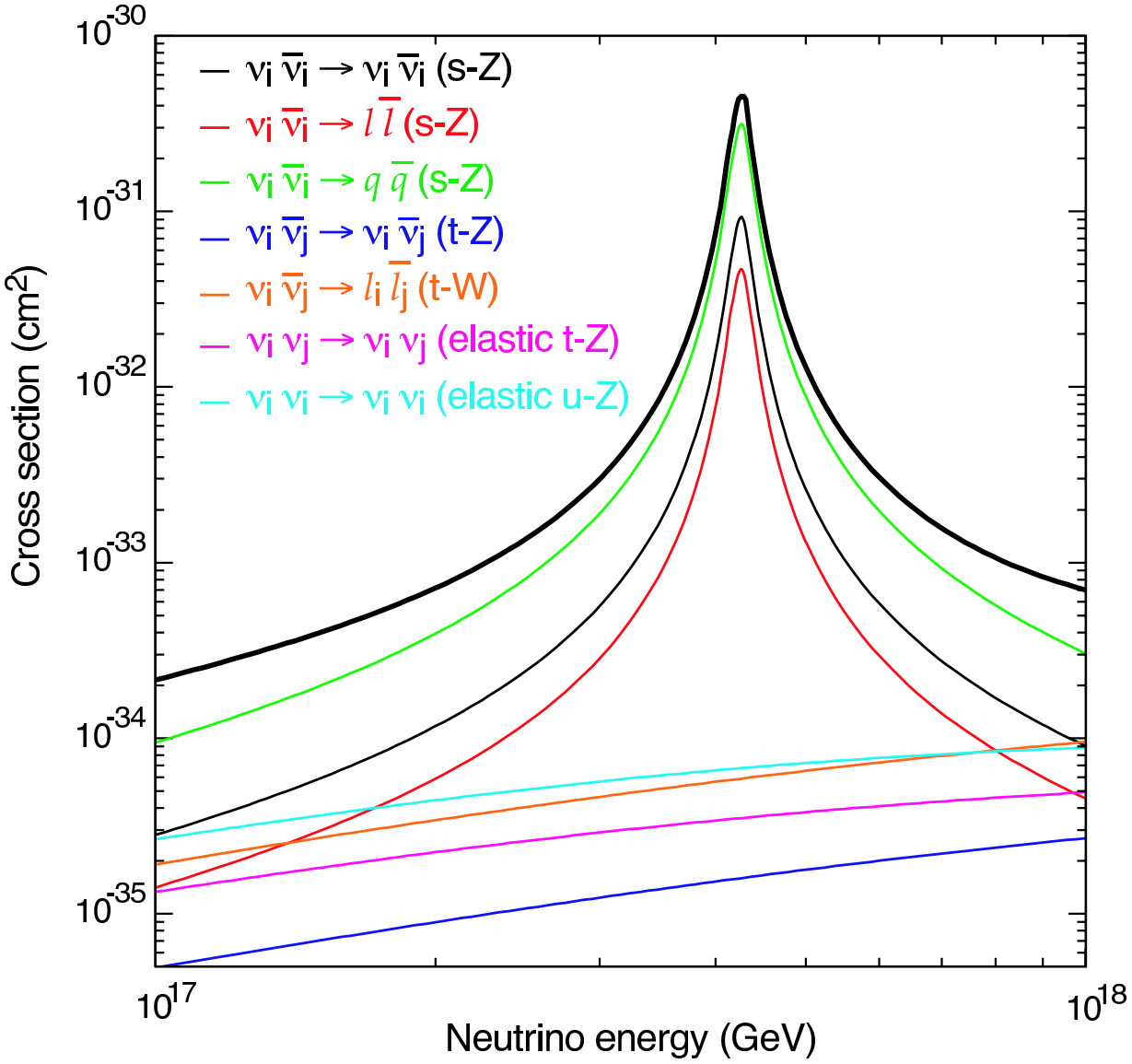
Energy-dependent composition as marker of ν decays



$E_\nu = \varepsilon(1\ \mathrm{s/eV})/(\tau_\nu/m_\nu) \cdot L/(100\ \mathrm{Mpc})$

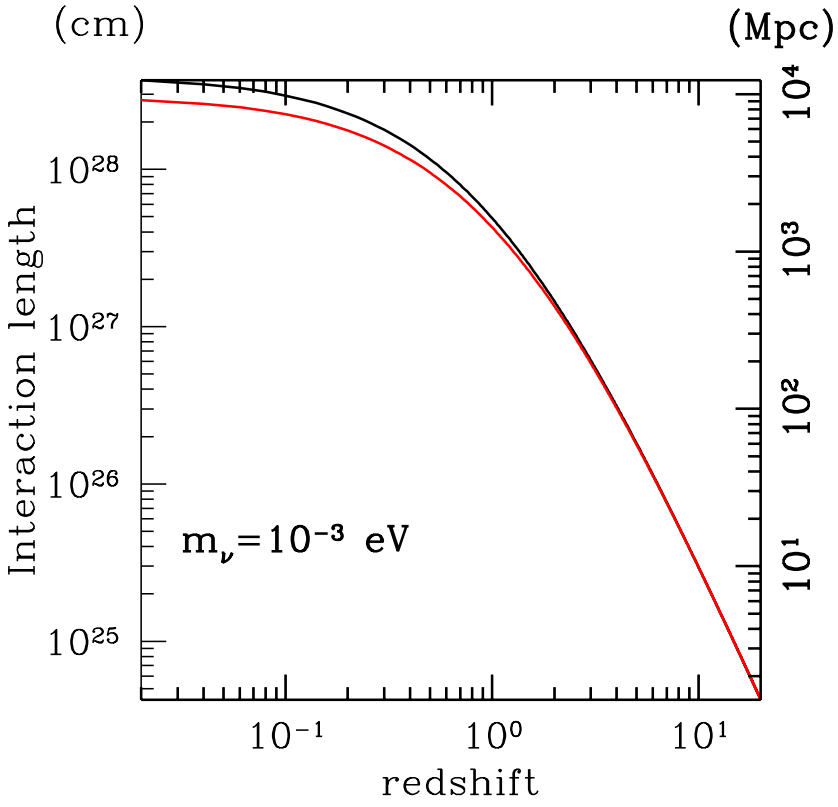
Inverted hierarchy

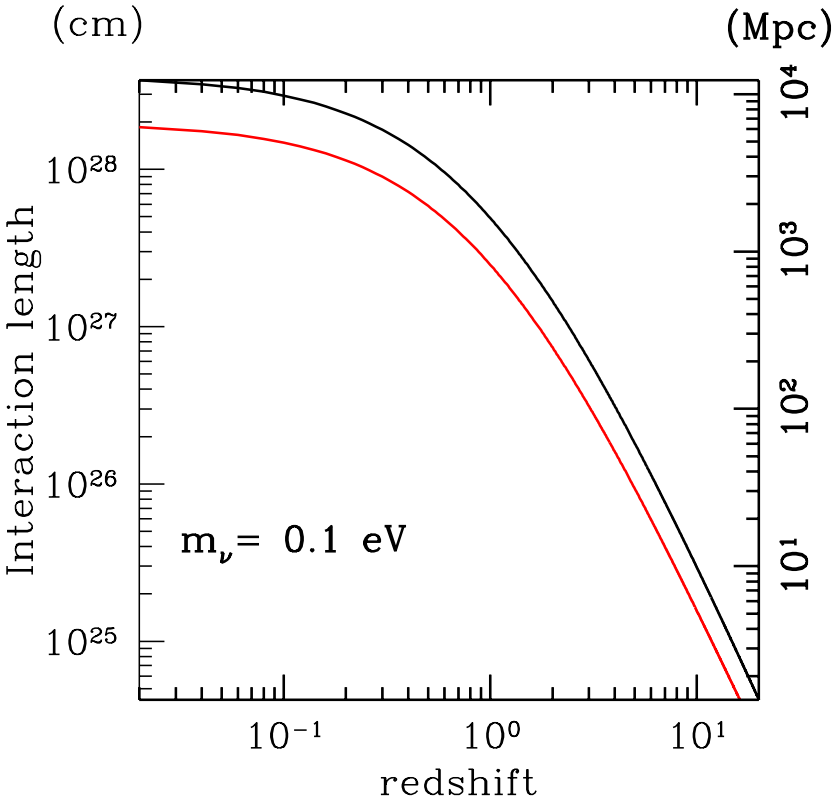
UHE ν annihilation on ν relics: $\nu\bar{\nu} \to Z$



$m_\nu = 10^{-5}$ eV

Interaction lengths on Z^0 resonance: Dirac Majorana

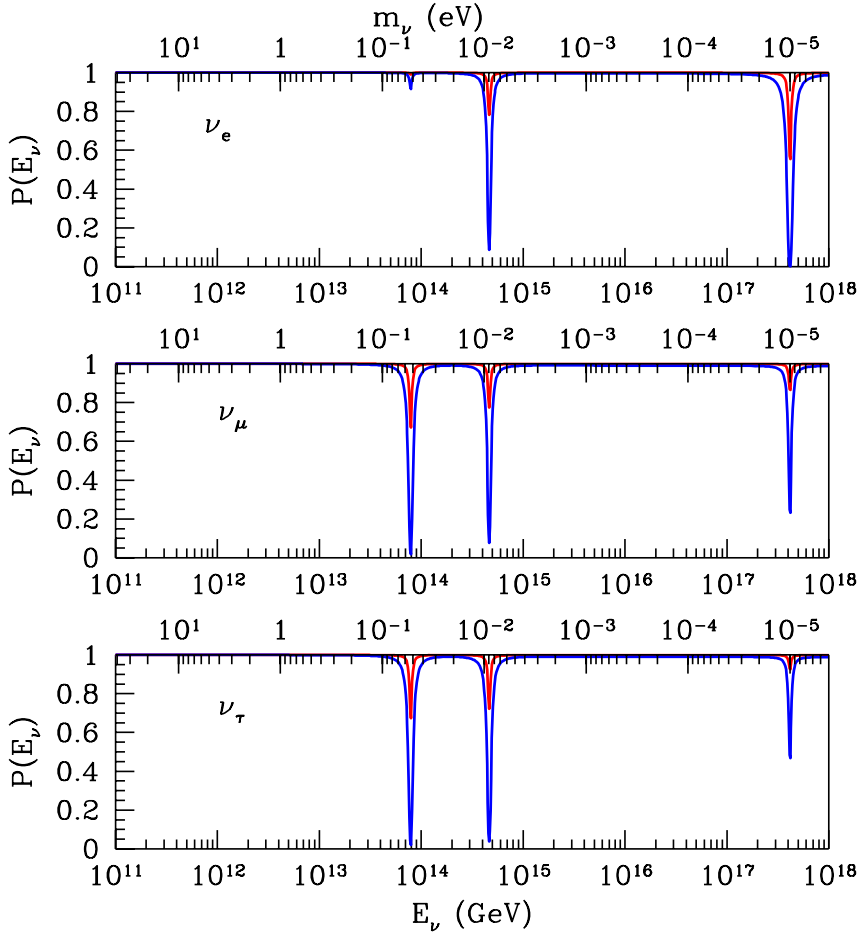




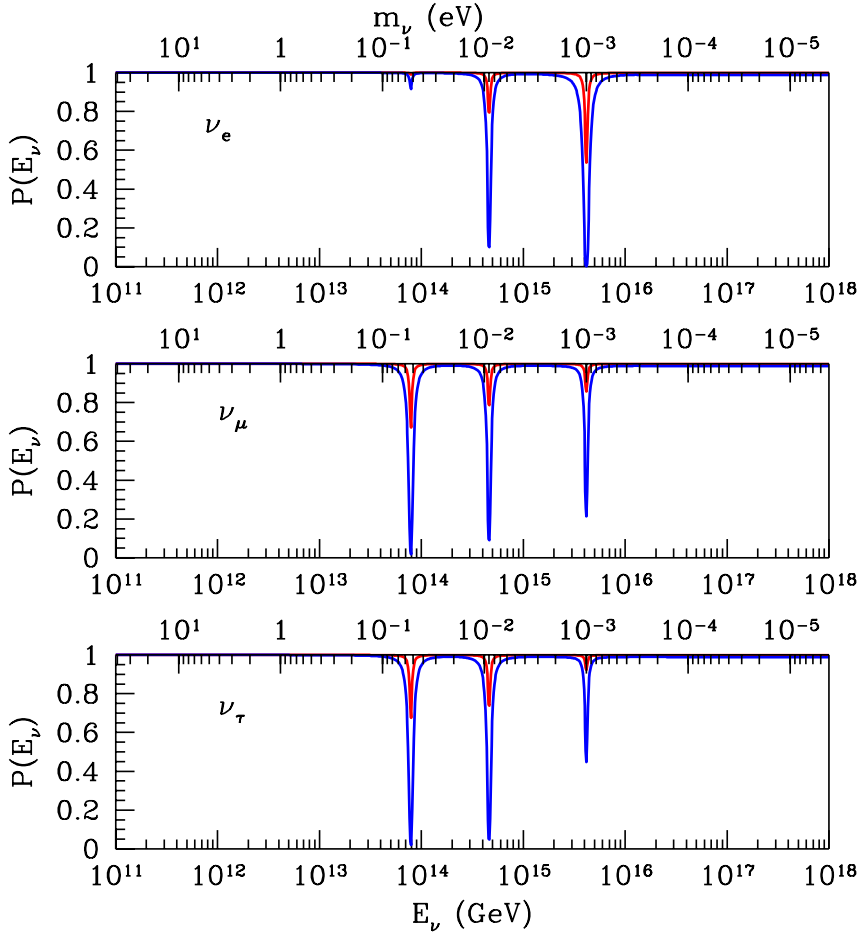
ν number density now: 56 cm^{-3}, $\propto (1+z)^3$

1.2×10^4 Mpc $=$ 39 Gly

Fable: l-o-o-o-o-o-n-g path (10^4 or 10^5 Mpc) in current U

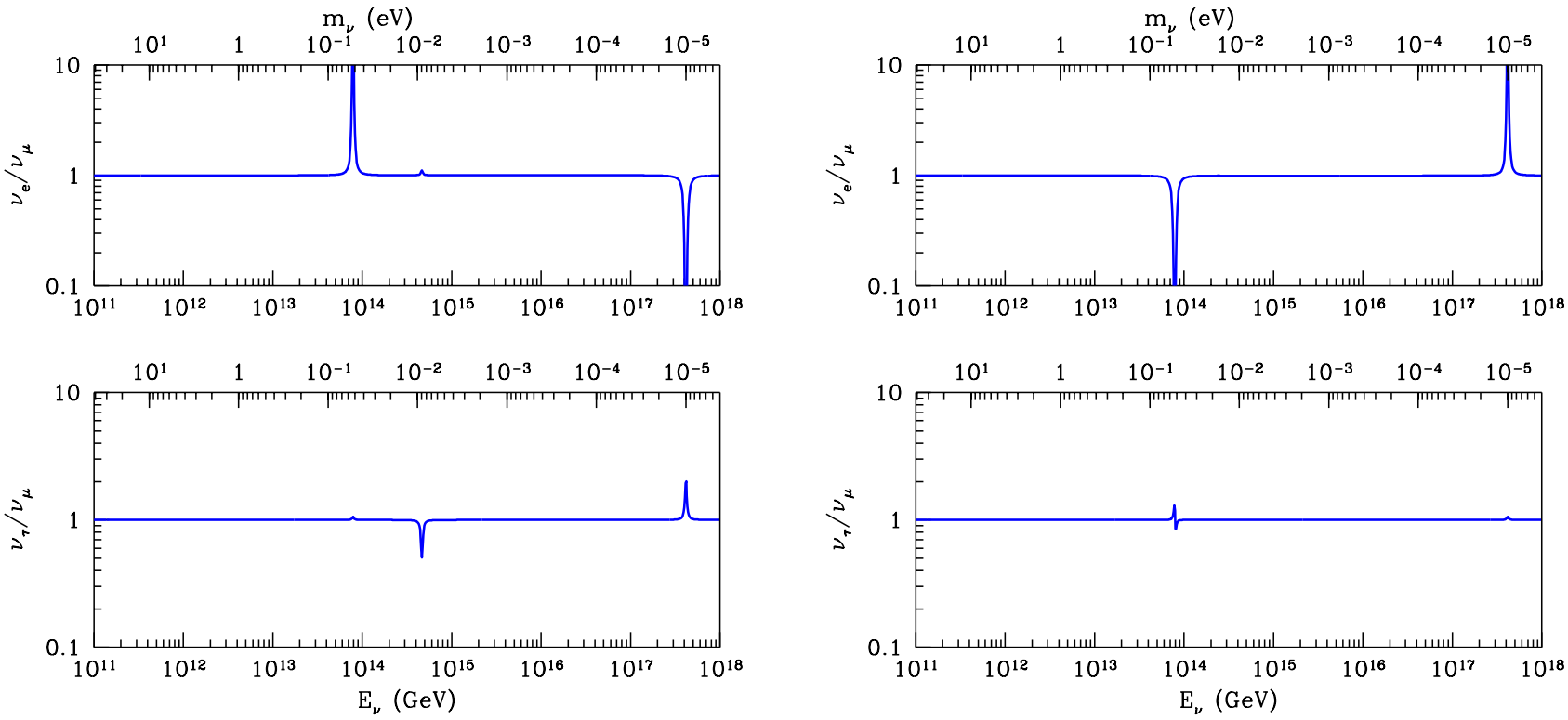


$m_\ell = 10^{-5}$ eV



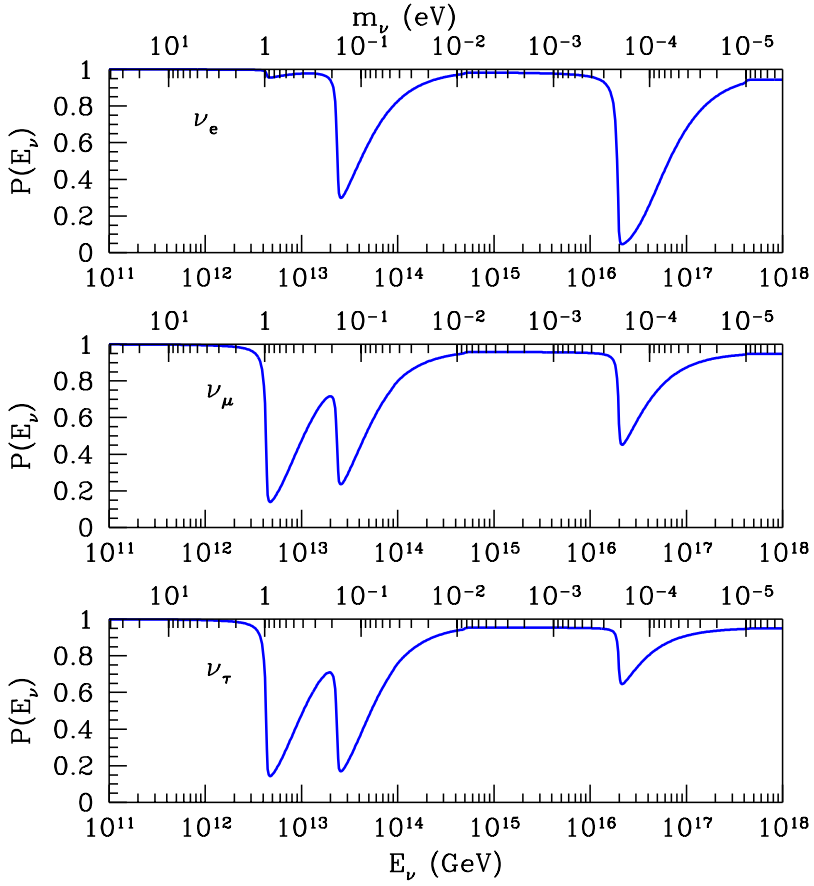
$m_\ell = 10^{-3}$ eV

Flavor ratios probe the mass hierarchy . . .

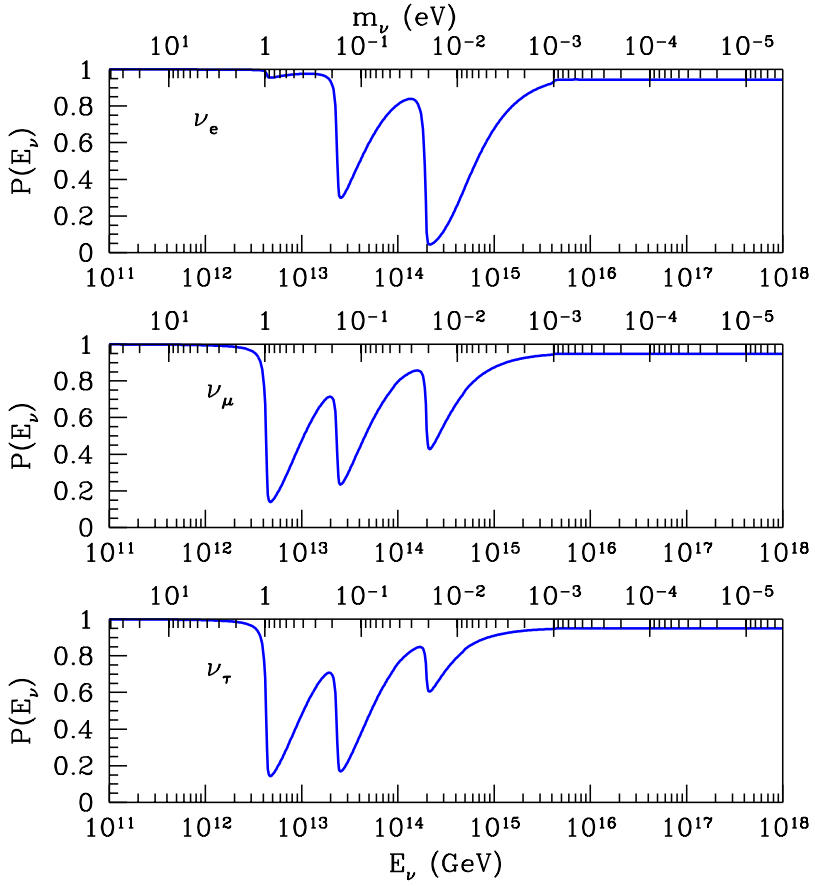


Normal $m_\ell = 10^{-5}$ eV Inverted

Incorporate evolution of U back to $z = 20$

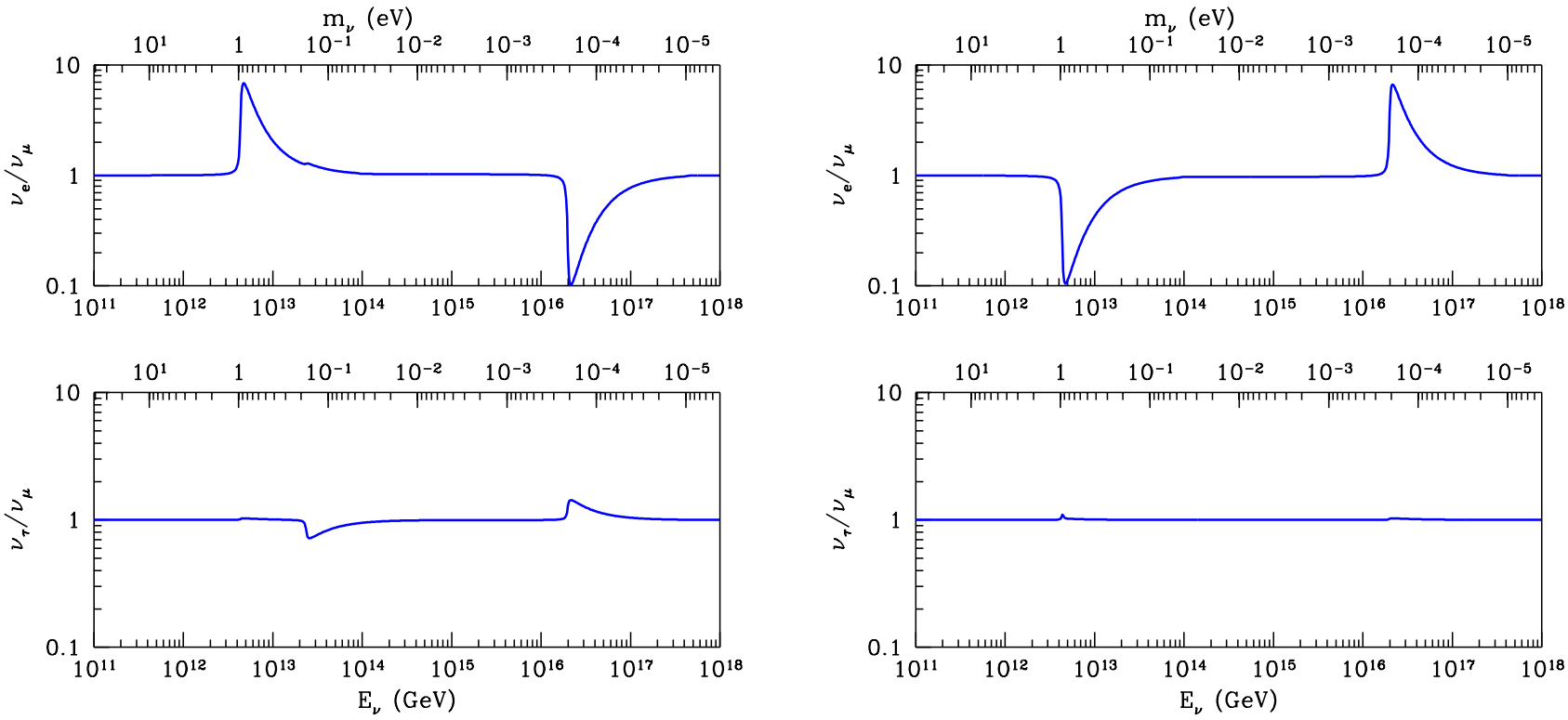


$m_\ell = 10^{-5}$ eV



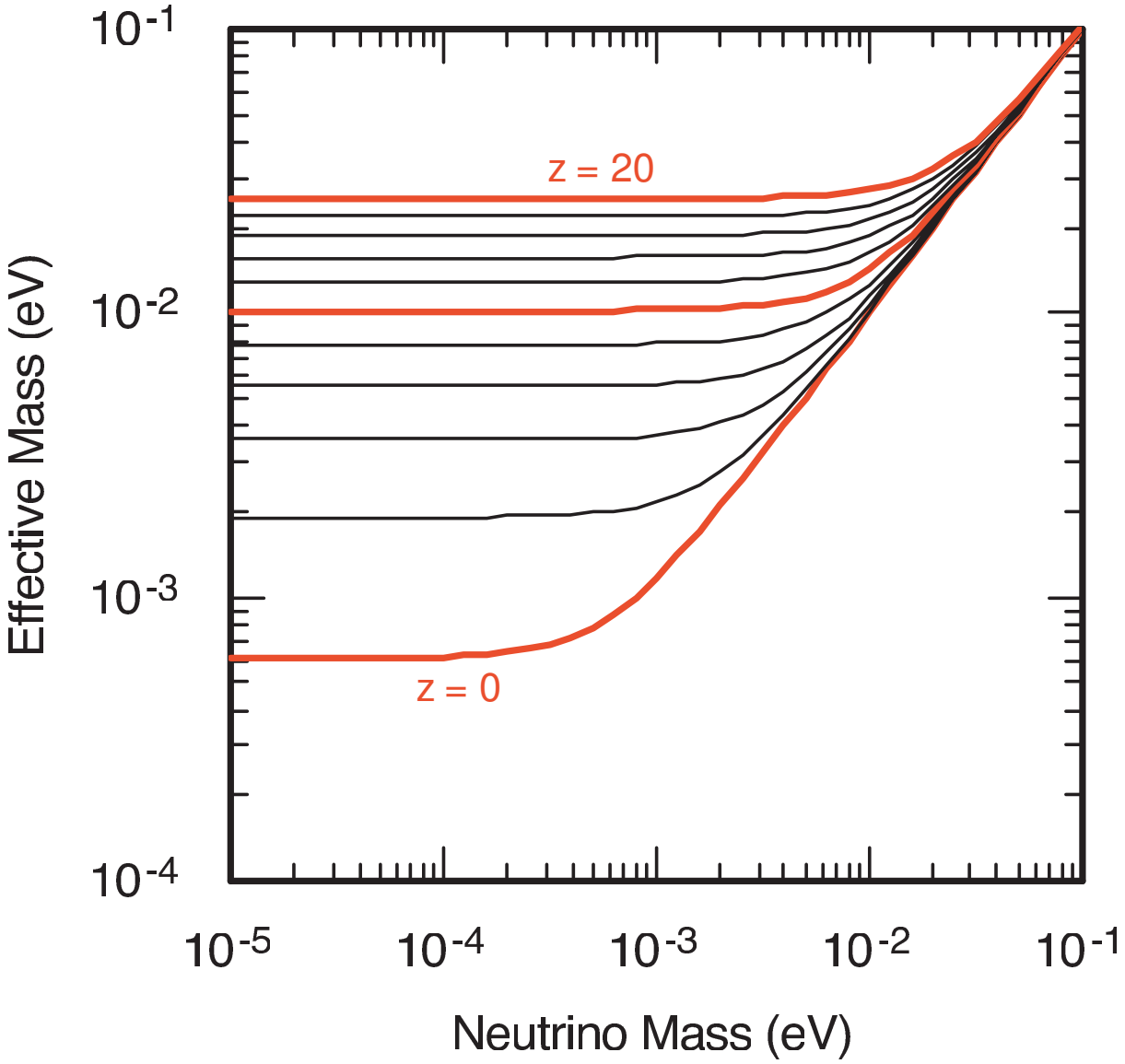
$m_\ell = 10^{-3}$ eV

Flavor ratios probe the mass hierarchy($z \lesssim 20$)



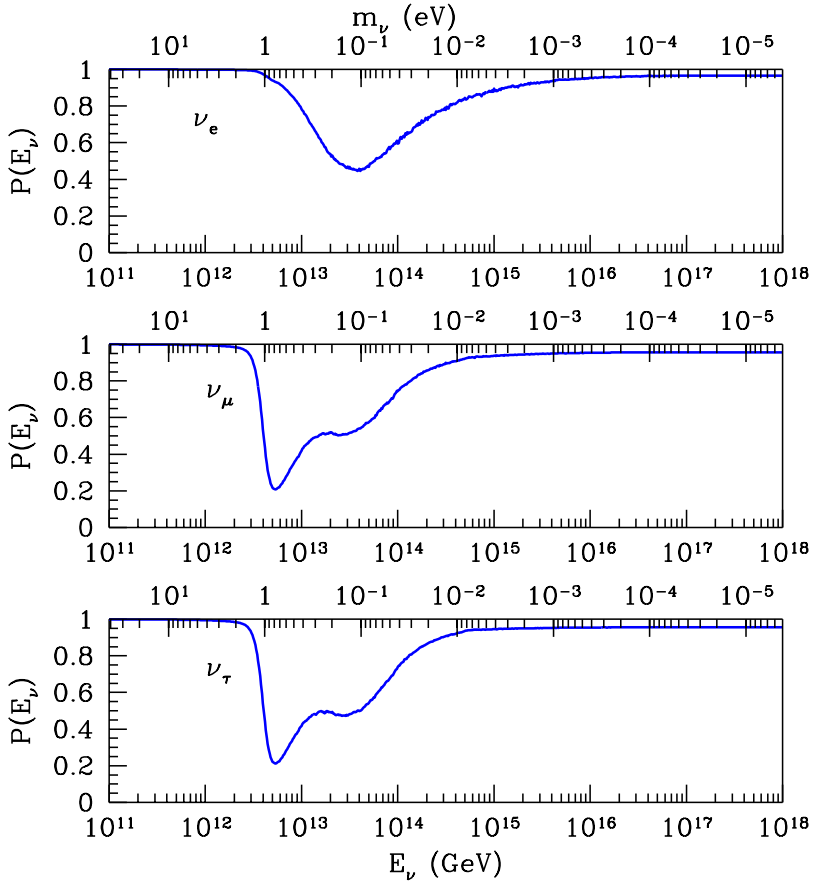
Normal $m_\ell = 10^{-5}$ eV Inverted

Relic neutrinos are moving targets . . .

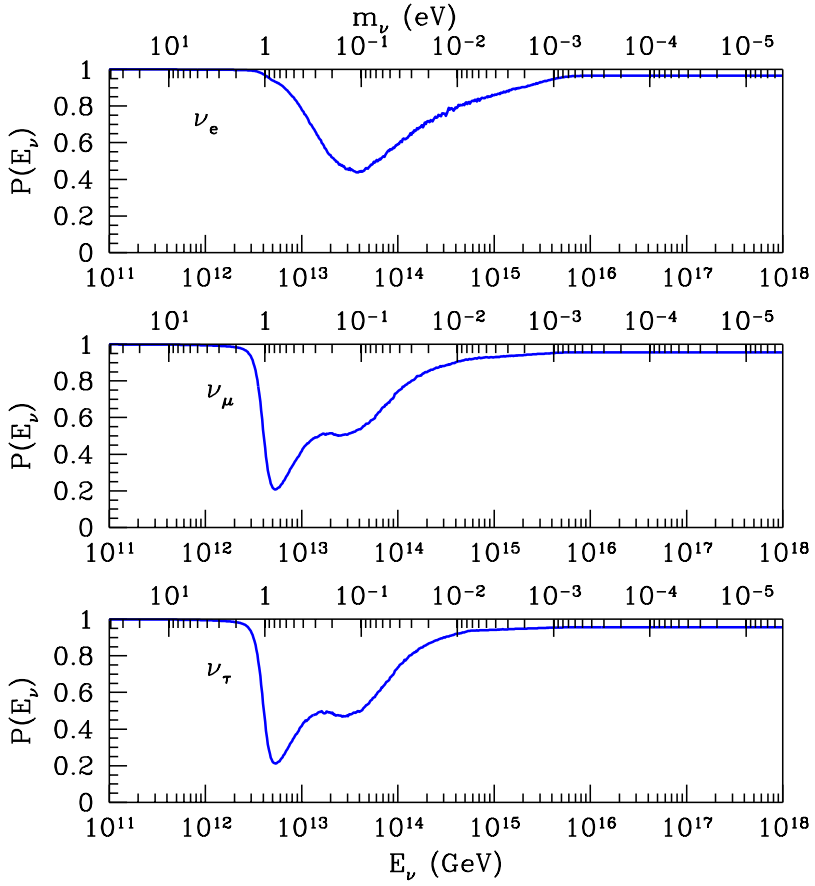


$$T_{\nu 0} = 1.945 \text{ K} = 1.697 \times 10^{-4} \text{ eV} \quad T_\nu \propto (1+z)$$

Incorporate evolution of U back to $z = 20$, Fermi motion

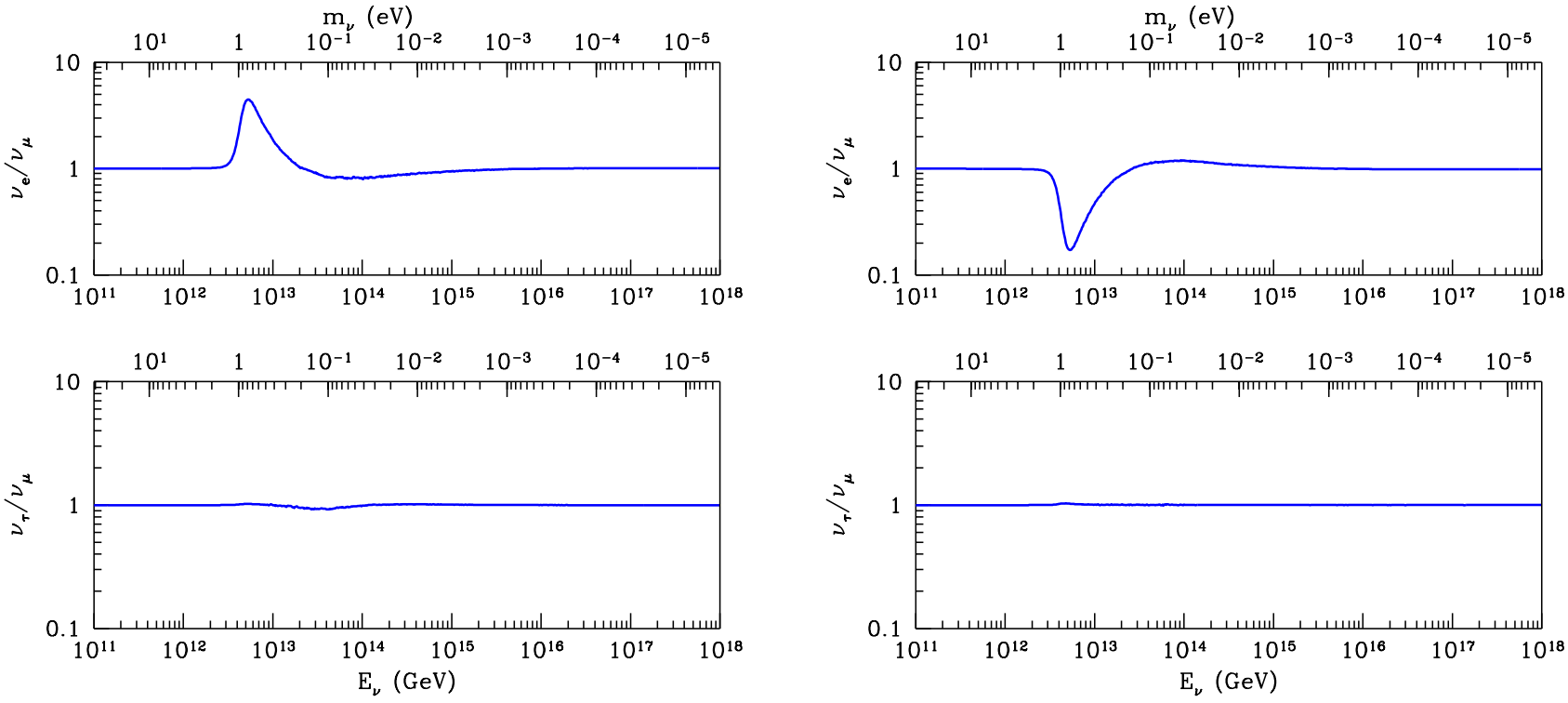


$m_\ell = 10^{-5}$ eV



$m_\ell = 10^{-3}$ eV

Flavor ratios probe mass hierarchy($z \lesssim 20$, Fermi motion)



Normal $m_\ell = 10^{-5}$ eV Inverted

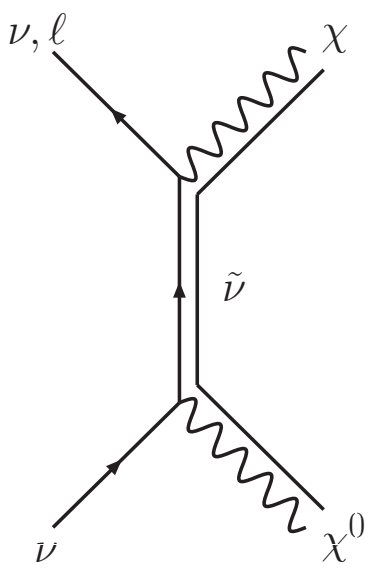
Neutrino Coannihilation on Dark-Matter Relics?

For neutralino dark matter, $M_{\chi_1^0} \approx 150$ GeV

Good news: $E_\nu^{\rm res} \approx 400$ GeV ($\tilde{\nu}$ formation);
cross section 10% of $\nu\bar{\nu} \to Z$

Bad news: relic χ^0 much rarer than relic ν
Universe at large: 56 ν cm^{-3}, $\lesssim 10^{-8}$ χ^0 cm^{-3}
Interaction length for $\tilde{\nu}$ formation: 10^{15} Mpc

Our location in galaxy [NFW]: $\lesssim 10^{-3}$ χ^0 cm^{-3}
Solar system, inside Earth orbit [Khriplovich & Pitjeva]: $<$350 χ^0 cm^{-3}



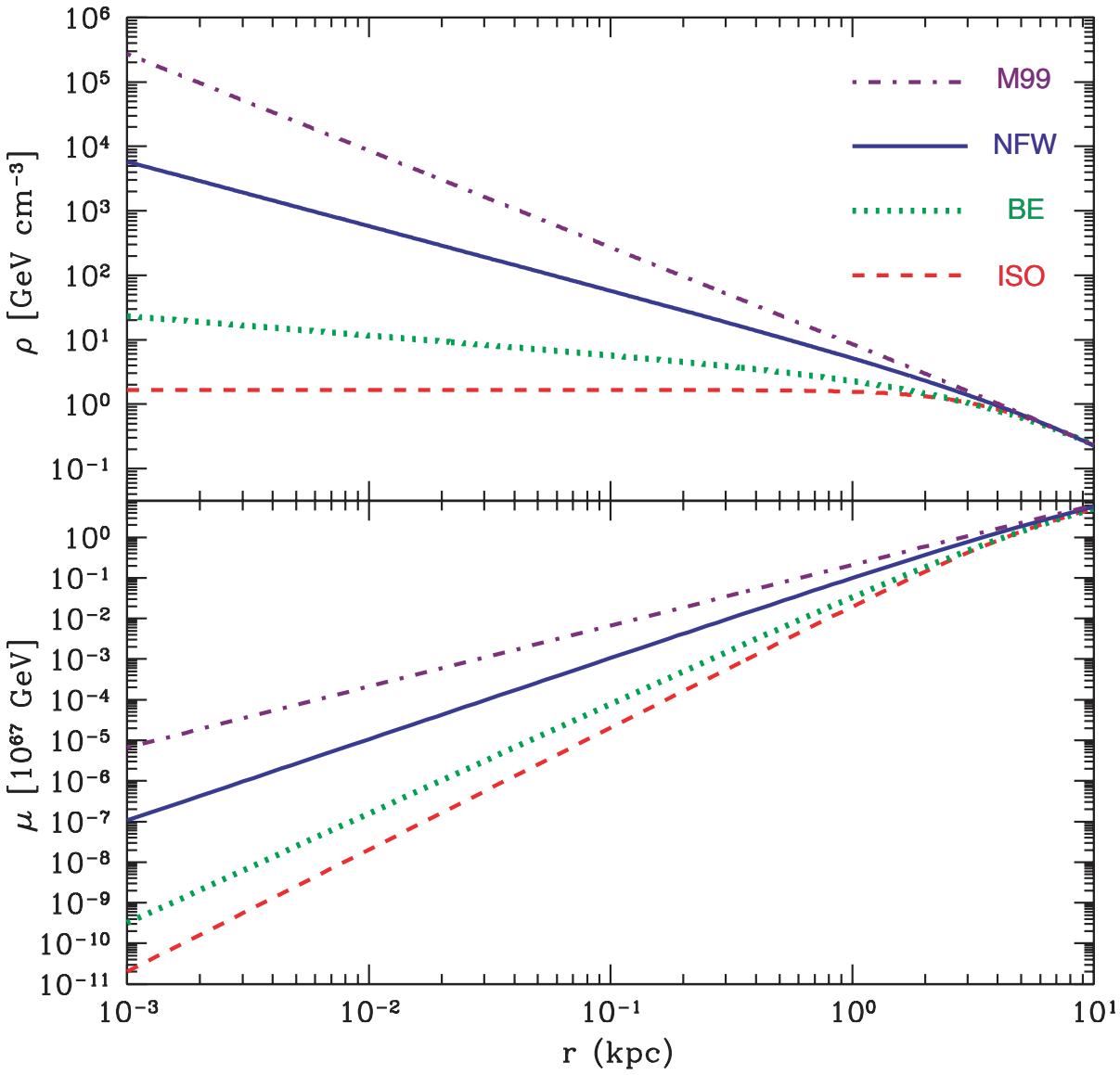
$\rightsquigarrow$ $< 10^{-6}$ $\tilde{\nu}$ y^{-1} in Earth's atmosphere (ATM ν)

...but up to $O(600)$ $\tilde{\nu}$ y^{-1} inside Earth's orbit (AGN ν)

Barenboim, Mena, CQ

Datta, Fargion, Mele: UHE χ^0 on relic ν

Dark-matter profiles for our galaxy . . .



$\ldots \nu\chi_1^0 \to \tilde{\nu}$

Entire galaxy would contain $\sim 10^{65}$ neutralinos (NFW profile)

With reasonable ν flux, $dN_\nu/dE_\nu \approx 5 \times 10^{-18}$ [GeV cm^2 s sr]$^{-1}$,

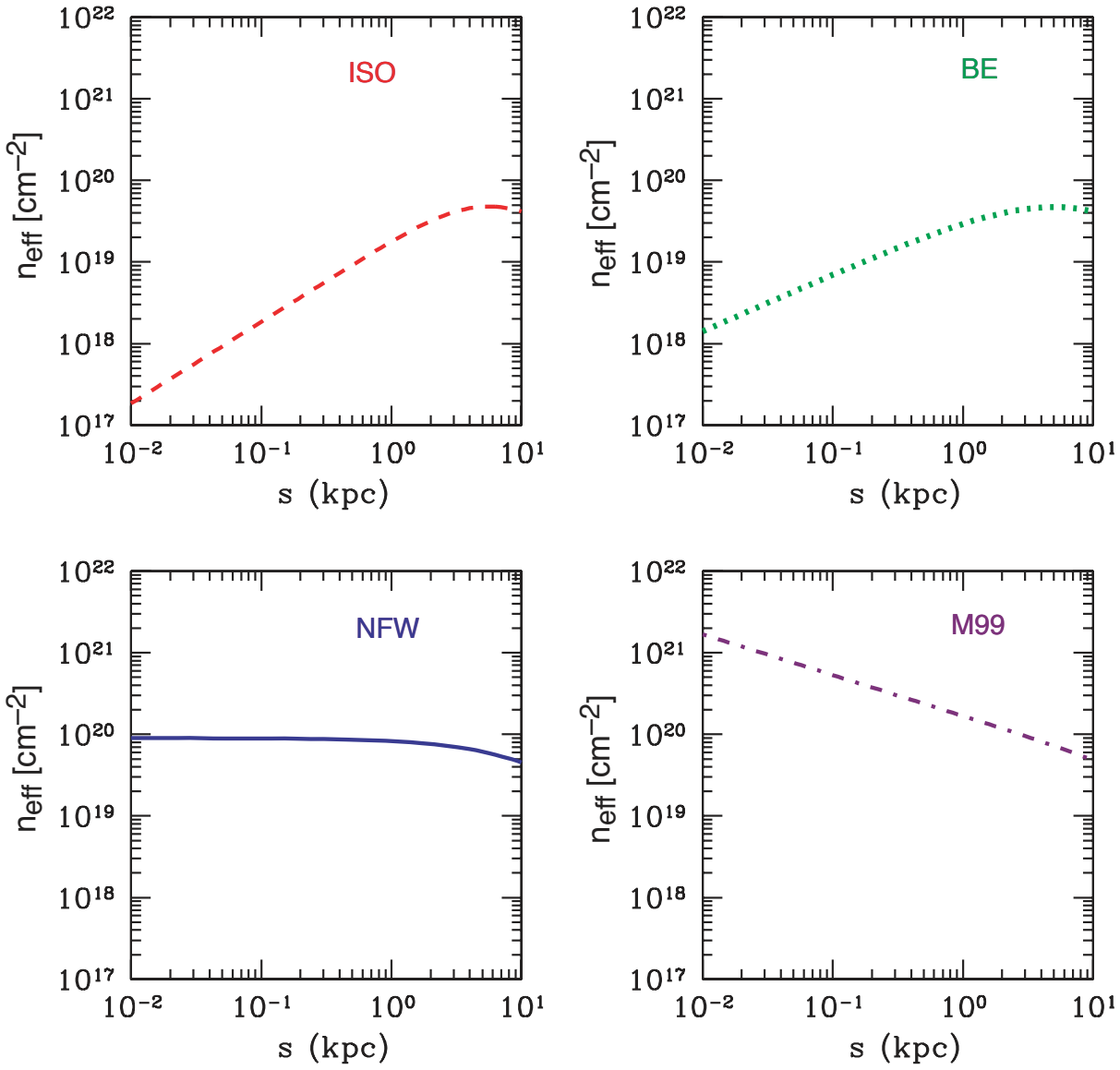
expect $O(10^{24})$ coannihilations per year in the galaxy

Few-GeV γ signals from inelastic decay channels, *most prominent for* ν_τ

...for the right kind of neutralino dark matter (GLAST regime)

...but we would detect only $O(10^{-21})$ cm^{-2} y^{-1} $\rightsquigarrow$ hopeless!

Effective number of targets viewed per detector area



Gravitational Lensing of Neutrinos?

How demonstrate neutrinos have normal gravitational interactions?

Pound–Rebka experiment exploiting Mössbauer effect? Raghavan

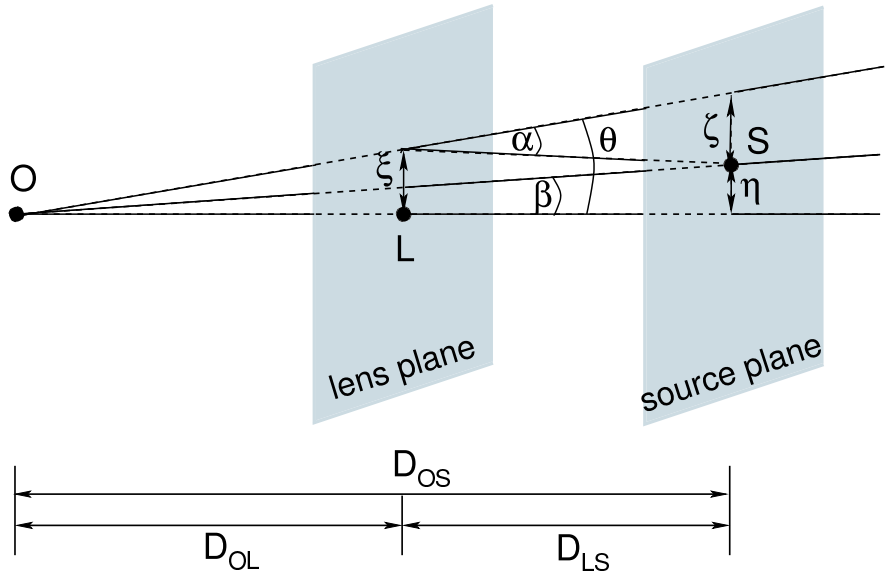
Arrival time of SN1987A ν, γ Longo, Krauss & Tremaine

Lack steady sources, angular resolution to see deflection by the Sun

Deflection $\alpha = 2\mathcal{R}/\xi \approx 6$ km$/700\,000$ km ≈ 8.5 μrad

$\mathcal{R}$: Schwarzschild radius; ξ: impact parameter

Lensing essentials



Lensing Supernova neutrinos by black hole at galactic center:

significant amplification, time dispersion

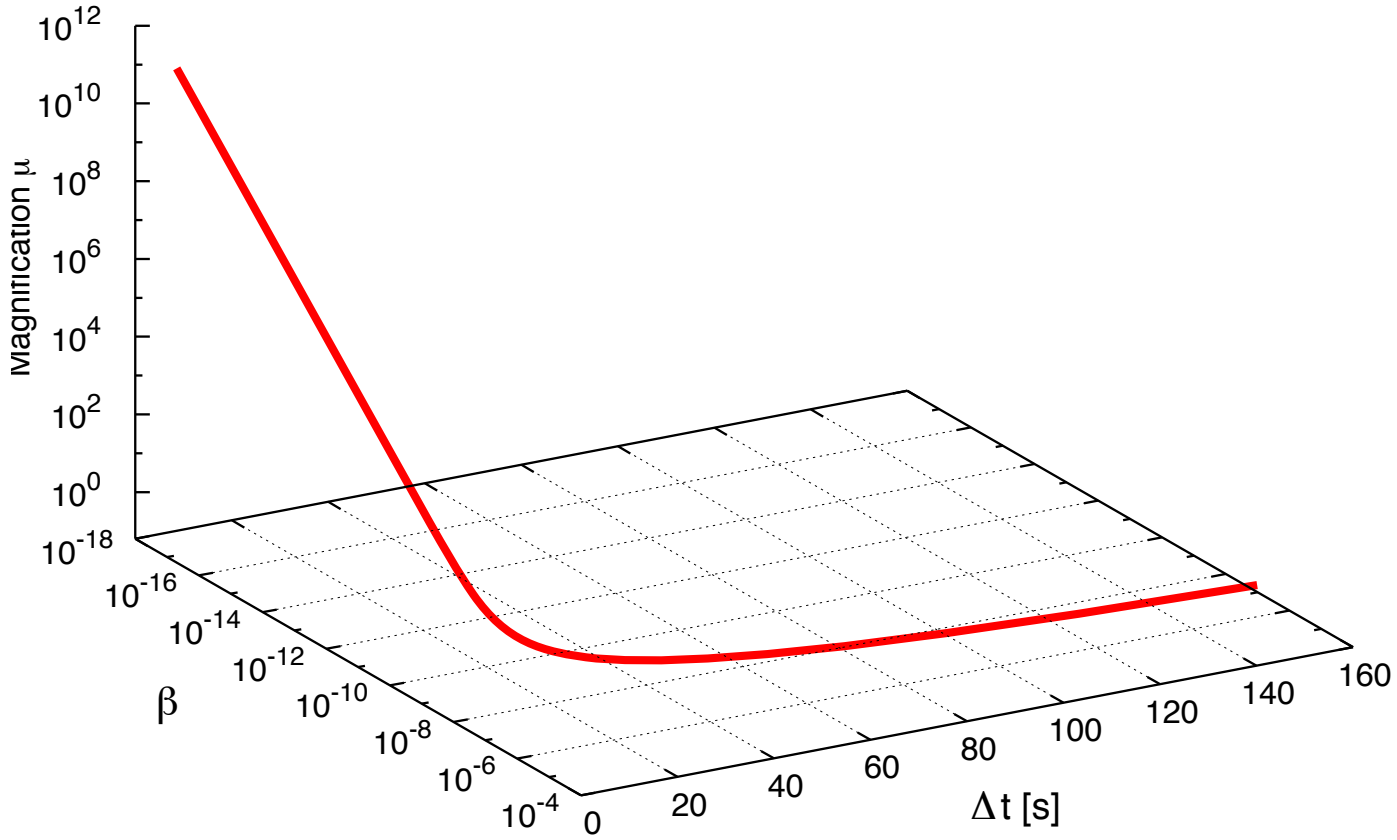
For symmetric case, β: misalignment angle, $\theta_{\rm E}^2 = 2\mathcal{R}/D_{\rm OS}$:

Magnification: $\mu \approx \theta_{\rm E}/\beta$ Time dispersion: $\Delta t \approx 142\ {\rm s} \cdot (\beta/\theta_{\rm E})$

10-km source radius, $\mu^{\rm max} \approx 10^{11}$ (!)

Mena, Mocioiu, CQ: astro-ph/0610918

Amplification / time dispersion



Do lensing events ever happen?

- Galactic SN $\rightsquigarrow$ ν-burst: 1 in 47 ± 12 y
- If core-collapse SNe track neutron stars in disc:
  $\approx 2 \times 10^{-6}$ of galactic SNe lensed toward Earth
  $\Rightarrow$ 180 lensed SNe over history of solar system
- $10\times$ amplification: 1 in 250 My
  $100\times$: once in history
  $\gtrsim 50$ s dispersion ($\mu \lesssim 3$): 1 in 38.5 My

"It is a part of probability that many improbable things will happen."
George Eliot (after Aristotle), *Daniel Deronda*

If we witnessed a lensing event . . .

- Galactic SN at 16 kpc distance: 3900 events in Super-K, without lensing
  Example lensed event: $\times 10$, $\Delta t \approx 15$ s
  (can record 30K events in first second)
- IceCube will record low-energy ν as excess photoelectrons, with excellent time resolution

Lensing in the historical record?

- Isotopic anomalies (Mo – Tc)?
  $\nu + {}^{97}\mathrm{Mo} \rightarrow {}^{97}\mathrm{Tc}\ (t_{1/2} = 2.6\ \mathrm{My}) + n + e^-$

  1 My integration time not well matched to frequency of lensed SNe
- Extinctions?
  Genetic damage from recoiling nuclei?

From Neutrino Astronomy to Particle Physics

Prospects for probing particle physics in neutrino telescopes will be greatly enhanced by

- recording, characterizing energy of NC events
- neutrino flavor tagging, with energy measurement
- attention to surprises (e.g., misplaced absorption lines)
- SN neutrino bursts from other side of our galaxy